



JOURNALOF NON-CRYSTALLINE SOLIDS "I Bigging Con-State of the Solid State I State of the Solid State of the Solid State I State of the Solid State of the Solid State I State of the Solid State of the Solid State of the Solid State I State of the Solid State

## Journal of Non-Crystalline Solids

journal homepage: www.elsevier.com/locate/jnoncrysol

# $BaF_2$ modified $Cr^{3\,+}/Ho^{3\,+}$ co-doped germanate glass for efficient 2.0 $\mu m$ fiber lasers



### X.L. Yang, W.C. Wang, Q.Y. Zhang\*

State Key Laboratory of Luminescent Materials and Devices, Institute of Optical Communication Materials, South China University of Technology, Guangzhou 510641, China

#### ARTICLE INFO

Keywords:  $Cr^{3+}/Ho^{3+}$  co-doped Germanate glasses  $BaF_2$  modifiers 2.0 µm fiber laser

#### ABSTRACT

The influence of BaF<sub>2</sub> on the physical and spectroscopic properties of  $Cr^{3+}/Ho^{3+}$  co-doped germanate glass is investigated systematically by differential scanning calorimeter, excitation and emission spectra, as well as dynamic decay lifetime. The intense and broad absorption band of  $Cr^{3+}$  provides a selective pump scheme for obtaining an efficient 2.0 µm emission of Ho<sup>3+</sup>, the OH<sup>-</sup> absorption coefficient, on the other hand, is decreased as low as 1.08 cm<sup>-1</sup>, which both highly conducive to obtain an intense 2.0 µm emission of Ho<sup>3+</sup>. In addition, the crystal-field parameter  $D_q/B$  of  $Cr^{3+}$ -doped glasses is also calculated to study the influence of BaF<sub>2</sub> on the local environment of activators and sensitizers. Further theoretic calculation shows that the largest absorption and emission cross-sections of Ho<sup>3+</sup> near 2.0 µm are as high as 4.6 and 5.2 (×10<sup>-21</sup> cm<sup>2</sup>) in the 10 mol% BaF<sub>2</sub> modified  $Cr^{3+}/Ho^{3+}$  co-doped glass and the maximum energy transfer efficiency from  $Cr^{3+}$  to Ho<sup>3+</sup> is about 42.5%. All results suggest that this BaF<sub>2</sub> modified  $Cr^{3+}/Ho^{3+}$  co-doped glass is very suitable for a high-efficient 2.0 µm fiber lasers with flexible pump sources.

#### 1. Introduction

In recent years, Ho<sup>3+</sup> ion has gained lots of significant interest for the development of 2.0 µm solid-state fiber lasers due to its relatively higher stimulated emission cross-section, longer decay lifetime and longer laser wavelength [1,2]. However, Ho<sup>3+</sup> ion suffers from a certain limitation of non-absorbing commercially available 808 nm or 980 nm laser diodes (LDs), a common approach to solving this problem is employing a series of appropriate rare-earth ion sensitizers to enhance the 2.0  $\mu$ m emission of Ho<sup>3+</sup>, such as Yb<sup>3+</sup> [3], Tm<sup>3+</sup> [4], Er<sup>3+</sup> [5], and  $Nd^{3+}$  [6]. Unfortunately, the sensitizing effect of current rareearth ions is strictly defined by their narrow excitation and emission bands [7]. As an excellent sensitizer, the *d*-*d* transitions of chromium ion are intensively investigated [8-13]. For example, in our previous work [7], the various valance of chromium  $(Cr^{3+}, Cr^{4+}, Cr^{6+})$  can be detected by the absorption spectra from the fluoride-sulfophosphate glasses [9]. Besides that, the  $Cr^{3+}$  and  $Cr^{6+}$  instead of  $Cr^{4+}$  have been observed in the germanate glasses [8]. It should be noted that only  $Cr^{3+}$ is beneficial for achieving efficient energy transfer process between  $Cr^{3+}$  and  $Ho^{3+}$  or  $Tm^{3+}$  ions [7,8]. The efficient 2.0  $\mu$ m fluorescence has been obtained in the Ho<sup>3+</sup>-doped glass sensitized by Cr<sup>3+</sup>, an interesting finding is that the intense and broad absorption band of Cr<sup>3+</sup> provides a selective pump scheme for obtaining an intense 2.0 µm

emission of  $\text{Ho}^{3+}$  [7]. In order to explore flexible pump sources and improve the pumping efficiency for  $\text{Ho}^{3+}$ , more efforts should be performed to further study the sensitizing mechanism between  $\text{Cr}^{3+}$  and  $\text{Ho}^{3+}$  and improve their energy transfer efficiency.

On the other hand, germanate glass has been considered as a proper laser glass host for  $\text{Ho}^{3+}$  ion, which owns a lower maximum phonon energy, outstanding chemical stability, thermal stability, and excellent solubility for the rare-earth ions [14–17]. Nevertheless, it is recognized that an oxygen bridging <sup>4</sup>Ge and <sup>6</sup>Ge is forming a hydrogen bond with an OH<sup>-</sup> group in germanate glass, which constitutes an impurity quenching center for mid-infrared luminescence [18–20]. The introduction of proper amounts of fluorides into germanate glass can transform the glass structure and suppress the OH<sup>-</sup> groups simultaneously [21]. In addition, the local environment of activators and sensitizers can be influenced by the incorporation of BaF<sub>2</sub>, which may produce a higher pump efficiency for achieving an efficient energy transfer process from Cr<sup>3+</sup> to Ho<sup>3+</sup>.

Based on the above research backgrounds and reasons, this paper creatively studies the  $BaF_2$  modified  $Cr^{3+}/Ho^{3+}$  co-doped germanate glass for efficient 2.0 µm fiber lasers. The influence of  $BaF_2$  on the physical and spectroscopic properties of  $Cr^{3+}/Ho^{3+}$  co-doped germanate glass was investigated systematically by differential scanning calorimeter, excitation and emission spectra, as well as dynamic decay

E-mail address: qyzhang@scut.edu.cn (Q.Y. Zhang).

https://doi.org/10.1016/j.jnoncrysol.2017.12.031

Received 31 October 2017; Received in revised form 15 December 2017; Accepted 16 December 2017 Available online 28 December 2017 0022-3093/ © 2017 Elsevier B.V. All rights reserved.

<sup>\*</sup> Corresponding author.

lifetime. A key finding is that the excitation spectra of  $Cr^{3+}$  can be easily tailored by the incorporation of BaF<sub>2</sub>, which ultimately makes a higher pump efficiency for achieving an efficient energy transfer process from  $Cr^{3+}$  to  $Ho^{3+}$ . In addition, the energy transfer efficiency from  $Cr^{3+}$  to  $Ho^{3+}$  is improved as high as 42.5%. All results suggest that this BaF<sub>2</sub> modified  $Cr^{3+}/Ho^{3+}$  co-doped glass is very suitable for a high-efficient 2.0 µm fiber lasers with flexible pump sources.

#### 2. Experiment

The glass compositions were  $(20-x)BaO-(14.9-y)Ga_2O_3-65GeO_2xBaF_2-0.1Cr_2O_3-yHo_2O_3$  (x = 0, 5, 10, 15, 20; y = 0, marked as BGG:Cr<sup>3+</sup>; x = 0, 5, 10, 15, 20; y = 1.0, marked as BGG:Cr<sup>3+</sup>, Ho<sup>3+</sup>, respectively). In addition, two glass samples 20BaO-15Ga\_2O\_3-65GeO\_2 (BGG), 20BaO-14Ga\_2O\_3-65GeO\_2-1Ho\_2O\_3 (BGG:Ho<sup>3+</sup>) were prepared as comparisons. The starting materials were extra pure anhydrous reagents of GeO\_2 (Civi-Chem 99.999%), Ga\_2O\_3 (Aladdin, 99.99%), BaCO\_3 (Aladdin, 99.99%), BaF\_2 (Aladdin, 99.99%), Cr\_2O\_3 (Aladdin, 99.95%), and Ho\_2O\_3 (Aladdin, 99.99%). A batch of 15 g starting materials was completely weighed and mixed. Afterwards, the mixtures were melted in an alumina crucible covered by an alumina lid inside an electric furnace at 1350 °C for 30 min in air. Then the melts were poured into a preheated stainless steel mold and annealed at 400 °C for 2 h. The annealed specimens were well cut and polished into about 1.5 mm thickness for subsequent measurements.

Differential scanning calorimeter (STA449C/3/MFC, Germany) was conducted with N2 as protected atmosphere at a heating rate of 10 K/ min. The transmission spectra were acquired on a Vector-33 FTIR spectrometer (Bruker, Switzerland). Near-infrared (800-1700 nm) emission and excitation spectra as well as the fluorescence decay curves were measured on FLS-920 spectrometer (Edinburgh Instruments Ltd.) using a 450 W Xe lamp at 619 nm or a 150 W microsecond pulsed lamp as excitation sources, respectively, a liquid nitrogen cooled R5509-72 photomultiplier (PMT) as the detector. Photoluminescence spectra were measured on a Triax 320 type spectrofluorometer (Jobin-Yvon Corp.) fitted with an InGaAs detector (900-1500 nm) and a PbSe detector (1800-2300 nm) using an 808 nm laser diode (LD) as the irradiation source. The luminescence decay curves for 2.0 µm emission were captured by a Tektronix TDS 3012c Digital Phosphor Oscilloscope with pulsed 808 nm LD. All the measurements were carried out at room temperature.

#### 3. Results and discussions

Glass forming region (GFR) is the basis of fabricating the barium gallo-germanate glass, which has been experimentally delivered in [22], as marked in Fig. 1(a) with blue lines. Nevertheless, many superfluous endeavors have been carried out to discover their experimental GFR and there is a critical point in finding the GFR via a more efficient way. In our previous report [23], the GFR was predicted for selecting an optimal glass composition. The calculated GFR is found at around eutectic points  $(T_1, T_2, T_3)$ , as shown in Fig. 1(a) with red lines, these points are correspondingly achieved from the points  $e_1$ ,  $e_2$ ,  $e_3$  that are obtained on the basis of the related binary phase diagram [23]. In comparison with the calculated and the experimental GFR [22], an apparent difference comes from the discrepancies of the referred binary phase diagram data and the preparation condition [23]. The considered point 1 (composition: 20BaO-15Ga<sub>2</sub>O<sub>3</sub>-65GeO<sub>2</sub>) [21] is located at both the experimental [22] and the calculated GFR, which basically signifies the glass stability of point 1. When the proper amount of BaF<sub>2</sub> is added in substitution of BaO, the modified glasses also keep good stability by the common melt-quenching preparation. In order to evaluate glass thermal stability, DSC curves are exploited to determine the glass characteristic temperatures such as the glass transition temperature  $T_{g}$ , glass crystallization temperature  $T_x$  and the criterion  $\Delta T$  $(\Delta T = T_x - T_g)$  [14]. Fig. 2 displays the DSC spectra of BGG:Cr<sup>3+</sup> with



Fig. 1. The experimental and calculated GFR of BGG glass. (For interpretation of the references to color in this figure, the reader is referred to the web version of this article.)



Fig. 2. DSC spectra of BGG and BGG:Cr<sup>3+</sup> glasses with different BaF<sub>2</sub> contents.

**Table 1** The typical temperatures ( $T_g$ ,  $T_x$ ,  $\Delta T$ ) of BGG and BGG:Cr<sup>3+</sup> glasses with different BaF<sub>2</sub> contents.

| Glass typical temperature             | BGG | 0%  | 5%  | 10% | 15% | 20% |
|---------------------------------------|-----|-----|-----|-----|-----|-----|
| $T_g (°C)$ $T_x (°C)$ $\Delta T (°C)$ | 648 | 643 | 619 | 592 | 569 | 556 |
|                                       | 738 | 762 | 734 | 715 | 694 | 690 |
|                                       | 90  | 119 | 115 | 123 | 125 | 134 |

different amounts of BaF<sub>2</sub>, the detailed values are shown in Table 1. Here, the declines of  $T_g$  and  $T_x$  are ascribed to the more loosely packed glass network with increasing BaF<sub>2</sub> content [21]. Besides, it is informed that  $\Delta T$  values for all the Cr<sup>3+</sup> doped samples are above 100 °C, confirming excellent thermal stability against crystallization [24,25]. Table 2 exhibits the basic physical properties of Cr<sup>3+</sup> or/and Ho<sup>3+</sup> doped glasses with different BaF<sub>2</sub> amounts. The more loosely packed glass network is inferred from the declines of the density and refractive index with increasing BaF<sub>2</sub> contents [21,26].

Fig. 3(a) depicts typical absorption bands of  $Ho^{3+}$  ions, which are

| Table 2   |                         |                   |                              |           |
|---|-------------------------|-------------------|------------------------------|-----------|
| The basic physical properties of Cr <sup>3+</sup> | or/and Ho <sup>3+</sup> | doped glasses wit | h different BaF <sub>2</sub> | contents. |

| Glass                   | Density (g·cm <sup>-3</sup> ) | Average molar weight<br>(g·mol <sup>-1</sup> ) | Calculated $Cr^{3+}$ (Ho <sup>3+</sup> ) concentration (10 <sup>20</sup> cm <sup>-3</sup> ) | Refractive index @<br>633 nm | $\alpha_{\rm OH}^{-}$ (cm <sup>-1</sup> ) | $N_{OH}^{-}$ (10 <sup>18</sup> cm <sup>-3</sup> ) |
|-------------------------|-------------------------------|--|---|------------------------------|---|---|
| 0% (Cr <sup>3+</sup> )  | 4.631                         | 135.5  | 0.411   | 1.710                        | 4.04                                      | 49.50   |
| 5%                      | 4.623                         | 134.4  | 0.410   | 1.703                        | 3.45                                      | 42.26   |
| 10%                     | 4.612                         | 133.3  | 0.409   | 1.688                        | 2.71                                      | 33.21   |
| 15%                     | 4.577                         | 132.2  | 0.406   | 1.680                        | 1.68                                      | 20.51   |
| 20%                     | 4.557                         | 131.1  | 0.404   | 1.668                        | 1.17                                      | 14.36   |
| $0\% (Cr^{3+}/Ho^{3+})$ | 4.680                         | 137.5  | 4.096   | 1.712                        | 3.88                                      | 47.62   |
| 5%                      | 4.675                         | 136.4  | 4.092   | 1.709                        | 3.33                                      | 40.82   |
| 10%                     | 4.648                         | 135.3  | 4.068   | 1.689                        | 2.07                                      | 25.39   |
| 15%                     | 4.595                         | 134.2  | 4.022   | 1.683                        | 1.37                                      | 16.79   |
| 20%                     | 4.566                         | 133.1  | 3.996   | 1.669                        | 1.08                                      | 13.28   |

respectively contributed to the transitions from the ground level of <sup>5</sup>I<sub>8</sub> to the excited state levels of <sup>5</sup>I<sub>7</sub>, <sup>5</sup>I<sub>6</sub>, <sup>5</sup>I<sub>5</sub>, <sup>5</sup>F<sub>5</sub>, (<sup>5</sup>S<sub>2</sub>, <sup>5</sup>F<sub>4</sub>), (<sup>5</sup>F<sub>2</sub>, <sup>3</sup>K<sub>8</sub>, <sup>5</sup>F<sub>3</sub>), and  $({}^{5}F_{1}, {}^{5}G_{6})$  [7]. The wide absorption bands of  $Cr^{3+}$  ion are apparently centered at 350, 440, and 640 nm. Bands around 440 nm and 640 nm are contributed to the transitions from the <sup>4</sup>A<sub>2</sub> ground state to  ${}^{4}T_{1}$  and  ${}^{4}T_{2}$  excited states of  $Cr^{3+}$  and 350 nm band is ascribed to  $Cr^{6+}$ , respectively [7]. The lack of 1200 nm band in the absorption spectra indicates no evidence of Cr<sup>4+</sup> in these germanate glasses [8]. Therefore, in this case, Cr<sup>3+</sup> is the main valance of chromium ion and a huge potential advantage of multi-wavelength pump scheme is supported by the whole broad bands around 330–850 nm of chromium ions. Fig. 3(b) donates the transmission spectra around 1700-3200 nm of Cr<sup>3+</sup>-doped samples with different BaF2 contents. The OH<sup>-</sup> absorption coefficient  $(\alpha_{OH}^{-})$  and concentration  $(N_{OH}^{-})$  of BGG:Cr<sup>3+</sup> with different BaF<sub>2</sub> contents are calculated [26] and displayed in Table 2. The OH<sup>-</sup> coefficient is lowered as low as  $1.08 \text{ cm}^{-1}$  after introducing 20% BaF<sub>2</sub> due to the chemical reaction of Ge-OH and BaF<sub>2</sub> [18], which is lower than that of some germanate glass  $(3.05 \text{ cm}^{-1})$  [27]. The inset represents the photograph of the samples, the visually green intensity of samples is distinctly faded when the amount of BaF2 increases at 15%. The color of samples changes in relation to the absorption band-shift of Cr<sup>3+</sup> in Fig. 3(c), the zoomed absorption band of  $Cr^{3+}$ :  ${}^{4}T_{2}$  shows a blue shift as

the amount of BaF<sub>2</sub> reaches 15% due to the apparently enhanced ionic bond around Cr<sup>3+</sup>. Moreover, the absorption bands of Cr<sup>3+</sup>:<sup>4</sup>T<sub>1</sub> and <sup>4</sup>T<sub>2</sub> with different BaF<sub>2</sub> contents are illustrated in Fig. 3(d). The absorption intensity of Cr<sup>3+</sup>:<sup>4</sup>T<sub>1</sub> is constantly reduced and the peak center of Cr<sup>3+</sup>:<sup>4</sup>T<sub>2</sub> shows a blue shift when the amount of BaF<sub>2</sub> increases at 15%. According to the Ref. [28], it has been pointed out that this absorption band shift of Cr<sup>3+</sup>:<sup>4</sup>T<sub>2</sub> is attributed to the spin-orbit coupling between <sup>4</sup>T<sub>2</sub>, <sup>2</sup>E, <sup>2</sup>T<sub>1</sub> excited states. When the content of BaF<sub>2</sub> reaches 15%, the overall excess of F<sup>-</sup> and Ba<sup>2+</sup> distinctly transforms the BaF<sub>2</sub> modified glass electronic structure where different spin multiplicities' states of Cr<sup>3+</sup> are interacted [28].

Table 3 shows the absorption band positions, Racah parameters *B* and *C*, crystal-field parameter  $D_q/B$  of different  $Cr^{3+}$  doped glasses, which are calculated based on the absorption positions [12]. According to the Ref. [29] that  $2.1 < D_q/B < 2.3$  distinguishes the low field from high field regions,  $D_q/B$  is slightly increased as BaF<sub>2</sub> content reaches 15%, which indicates that octahedral ligand field environment of  $Cr^{3+}$  is appropriately enhanced by fluorides [21]. Besides, on the basis of the  $3d^3$  configuration given by Tanabe-Sugano diagram [12], the increased value of  $D_q/B$  is close to the crossing point among the field-independent <sup>2</sup>E, <sup>4</sup>T<sub>2</sub>, and <sup>2</sup>T<sub>1</sub> energy curves [8]. Here, the anion type is changing as the substitution of BaF<sub>2</sub> is added, F<sup>-</sup> possesses a



**Fig. 3.** (a) Absorption spectra of  $Cr^{3+}$ -,  $Ho^{3+}$ -, and  $Cr^{3+}/Ho^{3+}$  co-doped germanate glasses (b) transmission spectra of  $Cr^{3+}$ -doped glasses (c) zoomed  ${}^{4}T_{2}$  absorption band and (d) absorption spectra of  $Cr^{3+}$ -doped glasses.

#### Table 3

| Absorption | band positions, | Racah parameters | B and C, crystal-field | d parameter $D_q/B$ | for Cr <sup>3+</sup> in BGG:Cr <sup>3+</sup> | <sup>+</sup> glasses with different Bal | <sup>7</sup> <sub>2</sub> contents and other glass hosts. |
|------------|-----------------|------------------|------------------------|---------------------|--|---|---|
|------------|-----------------|------------------|------------------------|---------------------|--|---|---|

| Glass     | $^{2}E (cm^{-1})$ | $^{2}\text{T}_{1} \text{ (cm}^{-1}\text{)}$ | $^{4}T_{2} (cm^{-1})$ | ${}^{4}T_{1} (cm^{-1})$ | $B  ({\rm cm}^{-1})$ | $C  ({\rm cm}^{-1})$ | $D_q/B$ | Ref.      |
|-----------|-------------------|---|-----------------------|-------------------------|----------------------|----------------------|---------|-----------|
| Fluoride  | 14,860            | 15,530                                      | 15,385                | 23,040                  | 850                  | 2948                 | 1.84    | [12]      |
| Phosphate | 14,660            | 15,870                                      | 15,270                | 22,370                  | 756                  | 3073                 | 2.02    | [12]      |
| 0%        | 14,354            | 15,249                                      | 15,527                | 23,026                  | 815                  | 2847                 | 1.90    | This work |
| 5%        | 14,354            | 15,249                                      | 15,527                | 23,026                  | 815                  | 2847                 | 1.90    |           |
| 10%       | 14,354            | 15,249                                      | 15,527                | 23,026                  | 815                  | 2847                 | 1.90    |           |
| 15%       | 14,354            | 15,249                                      | 15,724                | 23,026                  | 777                  | 2921                 | 2.02    |           |
| 20%       | 14,354            | 15,249                                      | 15,724                | 23,026                  | 777                  | 2921                 | 2.02    |           |

#### Table 4

Comparison of J-O parameters  $\Omega_t$  (t = 2, 4, 6) of Ho<sup>3+</sup> ions in various glass hosts.

| Glass           | $arOmega_t~(	imes 10^-)$ |            | Ref.       |           |
|-----------------|--------------------------|------------|------------|-----------|
|                 | $\Omega_2$               | $\Omega_4$ | $\Omega_6$ |           |
| Fluorophosphate | 2.10                     | 3.50       | 2.50       | [33]      |
| Gallate         | 5.70                     | 3.10       | 0.37       | [33]      |
| Germanate       | 3.30                     | 1.14       | 0.17       | [33]      |
| 0%              | 5.75                     | 3.18       | 0.92       | This work |
| 5%              | 5.62                     | 3.11       | 0.90       |           |
| 10%             | 5.53                     | 3.06       | 0.89       |           |
| 15%             | 5.42                     | 3.00       | 0.87       |           |
| 20%             | 5.35                     | 2.96       | 0.86       |           |

lower intensive electron density than  $O^{2-}$  does, and the larger value of  $D_q/B$  is assigned to the larger anion packing density [7].

Table 4 presents the Judd-Ofelt (J-O) parameters of Ho<sup>3+</sup> doped various glasses [30,31]. Three parameters ( $\Omega_{t}$  t = 2, 4, 6) appear in the order of  $\Omega_2 > \Omega_4 > \Omega_6$ , here,  $\Omega_2$  is related to the hypersensitive transition. The large value of  $\Omega_2$  indicates the larger line strength of the hypersensitive transition and covalency parameter of rare-earth ions [32]. Monotonically dropped  $\Omega_2$  accordingly reveals the decreased covalency around Ho<sup>3+</sup> ions. The Ho-F bond is more ionic than Ho-O bond due to the higher electronegativity of F(4.0) than O(3.44), which accounts for the constantly diminished  $\Omega_2$  as the amount of BaF<sub>2</sub> is added [26]. The rigidity of host glass is recommended by  $\Omega_6$ , and the decreased  $\Omega_6$  indicates the reducing mechanical properties of glasses [26]. Based on the J-O parameters [32,33], the radiative transition probabilities ( $A_r$ ), branching ratios ( $\beta$ ), and radiative lifetimes ( $\tau_r$ ) of  $Ho^{3+}$  doped glasses are shown in Table 5. The value of  $A_r$  slightly decreases with adding the substitution of BaF<sub>2</sub>. The  $A_r$  (81.0 s<sup>-1</sup>) of 20%  $BaF_2$  modified BGG:Cr<sup>3+</sup>/Ho<sup>3+</sup> sample is higher than that of germanate glass  $(39.7 \text{ s}^{-1})$  [33], and gallate glass  $(69.5 \text{ s}^{-1})$  [33]. Moreover, the radiative lifetimes  $(\tau_r)$  of Ho<sup>3+</sup>:  ${}^{5}I_7 \rightarrow {}^{5}I_8$  transition are constantly prolonged with increasing the substitution of BaF2 due to the reduced

 $A_r$  [26]. The results demonstrate that  $Cr^{3+}/Ho^{3+}$  co-doped germanate glasses modified by a proper amount of BaF<sub>2</sub> can be comparatively a promising candidate to achieve 2.0 µm laser output.

Fig. 4 shows the near-infrared luminescent spectra of the BGG:Cr<sup>3+</sup> with different BaF<sub>2</sub> contents pumped by Xe lamp at 619 nm and an 808 nm LD. The broad emissions around 878 and 1000 nm are enhanced with the substitution of BaF2 added due to the diminished OHcoefficient, both of them are attributed to  $Cr^{3+}$ :  ${}^{4}T_{2} \rightarrow {}^{4}A_{2}$  transition [7]. Meanwhile, Fig. 4(c) donates the normalized excitation spectra of Cr<sup>3+</sup> monitored at 878 and 1000 nm. The similar excitation bands prove the same transitions from  $Cr^{3+}$ . Besides, this apparent shift of emission spectra of Cr<sup>3+</sup> could be ascribed to the various excitation wavelengths of different powers and distinct photoresponse performances around the detection limit of the different detectors that R5509-72 PMT is for Xe lamp at 619 nm, InGaAs photoconductor for an 808 nm LD [7]. Besides, Fig. 4(d) donates the excitation spectra of  $Cr^{3+}$ doped glasses monitored at 878 nm with different amounts of BaF<sub>2</sub> added. The two broad bands around 450 and 650 nm are attributed to  $\operatorname{Cr}^{3+}: {}^{4}A_{2} \rightarrow {}^{4}T_{1}$  and  ${}^{4}A_{2} \rightarrow {}^{4}T_{2}$  transitions, moreover, the sensitively detected centre positions of excitation bands are constantly blueshifting due to the enhanced ionic bond as the electronegativity of F is larger than O.

Fig. 5(a) presents the near-infrared emission spectra of the BGG:Cr<sup>3+</sup>/Ho<sup>3+</sup> with different BaF<sub>2</sub> contents under the excitation of an 808 nm LD. The observed emissions can be divided into two bands around 1000 and 1200 nm, which are respectively attributed to Cr<sup>3+</sup>:  ${}^{4}T_{2} \rightarrow {}^{4}A_{2}$  and Ho<sup>3+</sup>:  ${}^{5}I_{6} \rightarrow {}^{5}I_{8}$  transitions. Besides, the lump around 1065 nm is contributed to the harmonic light of the high-powered 808 nm laser diode. In comparison with the Ho<sup>3+</sup> doped glass, there is accordingly energy transfer from Cr<sup>3+</sup> to Ho<sup>3+</sup>:  ${}^{5}I_{6}$  manifold. Besides, the radiative transitions of Cr<sup>3+</sup> and Ho<sup>3+</sup> are promoted by the substitution of BaF<sub>2</sub> due to the decreased OH<sup>-</sup> coefficient. Fig. 5(b) illustrates the excitation spectra of the Ho<sup>3+</sup> doped sample with different BaF<sub>2</sub> contents monitored at 1200 nm. The excited bands for Ho<sup>3+</sup> are enhanced and broadened by Cr<sup>3+</sup>, which originate from being singly

Table 5

The calculated electric dipole ( $A_{ed}$ ) and magnetic dipole ( $A_{md}$ ) transition probabilities, spontaneous radiative transition probabilities ( $A_r$ ), branching ratios ( $\beta$ ), and the radiative lifetimes ( $\tau_r$ ) in BGG:Cr<sup>3+</sup>/Ho<sup>3+</sup> with different BaF<sub>2</sub> contents.

| Sample | Initial state               | Final state                 | $A_{ed} (s^{-1})$ | $A_{md}$ (s <sup>-1</sup> ) | $A_r (s^{-1})$ | β (%) | $\tau_r$ (ms) |
|--------|-----------------------------|-----------------------------|-------------------|-----------------------------|----------------|-------|---------------|
| 0%     | <sup>5</sup> I <sub>7</sub> | <sup>5</sup> I <sub>8</sub> | 60.24             | 31.77                       | 92.01          | 100   | 10.87         |
|        | <sup>5</sup> I <sub>6</sub> | <sup>5</sup> I <sub>8</sub> | 131.50            |                             | 131.50         | 80.80 |               |
|        |                             | <sup>5</sup> I <sub>7</sub> | 15.22             | 16.04                       | 31.26          | 19.20 | 6.14          |
| 5%     | <sup>5</sup> I <sub>7</sub> | <sup>5</sup> I <sub>8</sub> | 58.58             | 31.60                       | 90.18          | 100   | 11.09         |
|        | <sup>5</sup> I <sub>6</sub> | <sup>5</sup> I <sub>8</sub> | 127.87            |                             | 127.87         | 80.61 |               |
|        |                             | <sup>5</sup> I <sub>7</sub> | 14.80             | 15.96                       | 30.75          | 19.39 | 6.30          |
| 10%    | <sup>5</sup> I <sub>7</sub> | <sup>5</sup> I <sub>8</sub> | 55.60             | 30.51                       | 86.10          | 100   | 11.61         |
|        | <sup>5</sup> I <sub>6</sub> | <sup>5</sup> I <sub>8</sub> | 121.41            |                             | 121.41         | 80.49 |               |
|        |                             | <sup>5</sup> I <sub>7</sub> | 14.03             | 15.40                       | 29.44          | 19.51 | 6.63          |
| 15%    | <sup>5</sup> I <sub>7</sub> | <sup>5</sup> I <sub>8</sub> | 53.75             | 30.18                       | 83.93          | 100   | 11.91         |
|        | <sup>5</sup> I <sub>6</sub> | <sup>5</sup> I <sub>8</sub> | 117.35            |                             | 117.35         | 80.29 |               |
|        |                             | <sup>5</sup> I <sub>7</sub> | 13.57             | 15.24                       | 28.81          | 19.71 | 6.84          |
| 20%    | <sup>5</sup> I <sub>7</sub> | <sup>5</sup> I <sub>8</sub> | 51.64             | 29.43                       | 81.08          | 100   | 12.33         |
|        | <sup>5</sup> I <sub>6</sub> | <sup>5</sup> I <sub>8</sub> | 112.77            |                             | 112.77         | 80.17 |               |
|        |                             | <sup>5</sup> I <sub>7</sub> | 13.04             | 14.86                       | 27.90          | 19.83 | 7.11          |
|        |                             |                             |                   |                             |                |       |               |



**Fig. 4.** Emission spectra upon the excitation of (a) Xe lamp at 619 nm and (b) 808 nm LD, (c) normalized excitation spectra monitored at 878 nm and 1000 nm or (d) monitored at 878 nm in  $Cr^{3+}$ -doped glasses with different  $BaF_2$  contents.

Fig. 5. (a) Near-infrared emission spectra (b) excitation spectra (c) mid-infrared emission spectra and (d) decay curves in  $\rm Cr^{3+}/Ho^{3+}$  co-doped glasses.

confined to widely broadened ranging from 350 nm near to 800 nm. This signifies energy transfer(ET) from  $Cr^{3+}$  to  $Ho^{3+}$  and a large range of pump sources is expected to be applied. Besides, there are different phenomena of the excitation positions of  $Cr^{3+}$  and  $Ho^{3+}$  influenced by adding BaF<sub>2</sub>. The sensitive *d*-*d* transitions of  $Cr^{3+}$  distinctly move towards the short wavelength, however, the *f*-*f* transition manifolds of

Ho<sup>3+</sup> are mainly confined and populated by Cr<sup>3+</sup>. Fig. 5(c–d) demonstrates the luminescent spectra and the decay curves of 2.0 µm emissions in the BGG:Cr<sup>3+</sup>/Ho<sup>3+</sup> with different BaF<sub>2</sub> contents. The emission band of 2.0 µm is attributed to Ho<sup>3+</sup>: <sup>5</sup>I<sub>7</sub>  $\rightarrow$  <sup>5</sup>I<sub>8</sub> transition. The largest fluorescence intensity is located at the 10% amount of BaF<sub>2</sub> modified sample. The result indicates that the proper amount of BaF<sub>2</sub> is



Fig. 6. (a) The absorption and emission cross-sections (b) estimated gain coefficients corresponding to  ${\rm Ho^{3+}}$ :  ${\rm ^5I_7} \rightarrow {\rm ^5I_8}$  transition in BGG:Cr^{3+}/Ho^{3+} with 10% BaF\_2 content.

Table 6

Spectroscopic properties of  $Ho^{3+}$ :  ${}^{5}I_{7}$  level in BGG:  $Cr^{3+}/Ho^{3+}$  with 10% BaF<sub>2</sub> content and other glasses.

| Glass           | $Ho^{3+}$ ions ( $10^{20} cm^{-3}$ ) | λ (nm) | $\tau_m$ (ms) | FWHM (nm) | $\sigma_e^{FL} (10^{-21} \text{ cm}^2)$ | FWHM $\times \sigma_e^{FL}$ (10 <sup>-26</sup> cm <sup>2</sup> ) | Ref.      |
|-----------------|--------------------------------------|--------|---------------|-----------|---|--|-----------|
| Fluoride        | 2                                    | 2035   | 26.70         | 118       | 5.3                                     | 6.25   | [33]      |
| Silicate        | 2                                    | 2040   | 0.32          | 82        | 7.0                                     | 5.74   | [33]      |
| Germanate       | 2                                    | 2045   | 0.36          | 84        | 4.0                                     | 3.36   | [33]      |
| Fluorophosphate | 2                                    | 2035   | 5.60          | 123       | 7.9                                     | 9.72   | [33]      |
| 10%             | 4                                    | 2047   | 2.57          | 175       | 5.2                                     | 9.10   | This work |



Fig. 7. Simplified energy diagram of  ${\rm Cr}^{3+}/{\rm Ho}^{3+}$  co-doped glass as well as the quenching effect of  ${\rm OH}^-.$ 

#### Table 7

Calculated non-radiative probabilities of  ${\rm Ho^{3+:}5I_7}$  level for different amounts of  ${\rm BaF_2}$  modified samples and other glasses.

| Sample  | ZBLAN     | Silicate    | 0%            | 5%         | 10% | 15% | 20% |
|---|-----------|-------------|---------------|------------|-----|-----|-----|
| <i>W</i> <sub>nr</sub> (s <sup>-1</sup> )<br>Ref. | 4<br>[37] | 359<br>[38] | 562<br>This w | 531<br>ork | 303 | 197 | 151 |

10%. Besides, the measured lifetimes ( $\tau_m$ ) of 2.0 µm are determined as 1.53 ms, 1.61 ms, 2.57 ms, 3.56 ms, 4.31 ms, increased with the substitution of BaF<sub>2</sub> added due to the diminished quenching center of OH<sup>-</sup> groups.

The absorption ( $\sigma_a(\lambda)$ ) and emission ( $\sigma_e^{FL}(\lambda)$ ) cross-sections of Ho<sup>3+</sup>:2.0 µm are respectively determined by the Lambert-Beer law and Fuchtbauer-Ladenburg (FL) equation [32], as depicted in Fig. 6(a). The  $\sigma_a(\lambda)$  of Ho<sup>3+</sup>: <sup>5</sup>I<sub>8</sub>  $\rightarrow$  <sup>5</sup>I<sub>7</sub> transition in BGG:Cr<sup>3+</sup>/Ho<sup>3+</sup> with 10%

amount of BaF<sub>2</sub> is calculated as 4.6  $\times$  10<sup>-21</sup> cm<sup>2</sup> at 1950 nm,  $\sigma_e^{FL}(\lambda)$  is  $5.2 \times 10^{-21}$  cm<sup>2</sup> at 2047 nm, and FWHM is as wide as 175 nm. Meanwhile, FWHM  $\times \sigma_e^{FL}(\lambda)$  is an important parameter for estimating gain properties, the larger value generally represents a wider bandwidth and a higher gain character. Table 6 displays the spectroscopic properties of Ho<sup>3+</sup> near 2.0 µm in different glass hosts, and our sample has an advantage among the others. Fig. 6(b) shows the gain crosssection spectra (G( $\lambda$ )) of BGG:Cr<sup>3+</sup>/Ho<sup>3+</sup> with 10% amount of BaF<sub>2</sub>, which is computed by  $G(\lambda) = N \times [P \times \sigma_e^{FL}(\lambda) - (1 - P) \times \sigma_a(\lambda)]$ [26], where *P* is the population inversion given by the population ratio among the upper and lower manifolds. N is the calculated ion concentration of  $\text{Ho}^{3+}$  and determined as  $4.068 \times 10^{20} \text{ cm}^{-3}$ . With varying a set of P values from 0 to 1, the gain cross-section spectra are calculated and depicted versus the wavelength. Obviously, when P is at around 0.4, the positive gain occurs. The maximum gain coefficient of Ho<sup>3+</sup>:  ${}^{5}I_7 \rightarrow {}^{5}I_8$  transition is 2.06 cm<sup>-1</sup>, which is larger than that of some lead silicate glasses  $(0.89 \text{ cm}^{-1})$  [34], fluorophosphate glasses  $(0.74 \text{ cm}^{-1})$  [35], and silica-germanate glass  $(1.9 \text{ cm}^{-1})$  [36].

Based on the above results and Tanabe-Sugano diagram [12], a possible energy transfer mechanism [7,26] between  $Cr^{3+}$  and  $Ho^{3+}$  ions is illustrated in Fig. 7. The effects of spin-orbit coupling and electron-vibration interaction mix the  ${}^{4}T_{2}$  and  ${}^{2}E$  levels together [8]. The  ${}^{2}E$  level separates the 619 and 808 nm pump channels due to the energy difference. Populations on  $Cr^{3+}$ :<sup>4</sup>A<sub>2</sub> state are initially pumped to the <sup>4</sup>T<sub>2</sub> state, then ions on the  ${}^{4}T_{2}$  decay to the  ${}^{4}A_{2}$  state with 878 and 1000 nm emissions under the excitations of Xe lamp at 619 nm or an 808 nm LD, respectively. Furthermore, ions on the <sup>4</sup>T<sub>2</sub> manifold are derived from the <sup>4</sup>A<sub>2</sub> state via the excitations of 619 or 808 nm pump sources, then the energy transfers (ET1:  $\text{Cr}^{3+}$ : $^{4}\text{T}_{2}$  +  $\text{Ho}^{3+}$ : $^{5}\text{I}_{8} \rightarrow \text{Cr}^{3+}$ : $^{4}\text{A}_{2}$  +  $\text{Ho}^{3+}$ : $^{5}\text{I}_{6}$ ) to the adjacent Ho<sup>3+</sup>:<sup>5</sup>I<sub>6</sub> state [7] after the addition of Ho<sup>3+</sup>. The ions on the  ${}^{5}I_{6}$ state degenerate to the <sup>5</sup>I<sub>8</sub> ground manifold with 1200 nm emission or non-radiatively decay to the <sup>5</sup>I<sub>7</sub> state quenched by OH<sup>-</sup> groups (ET2:  $\text{Ho}^{3+}$ :  ${}^{5}\text{I}_{6} \rightarrow \text{OH}^{-}$ ). Meanwhile, ions on the  ${}^{5}\text{I}_{7}$  manifold decay to the  ${}^{5}\text{I}_{8}$ state with delivering 2.0 µm emission, partly depopulate to the OHgroups (ET3:  $Ho^{3+}: {}^{5}I_{7} \rightarrow OH^{-}$ ). As the amount of  $BaF_{2}$  is monotonously added, the OH<sup>-</sup> coefficient is lowered and the energy transfers from  $Ho^{3+}$ :  ${}^{5}I_{6}$  or  ${}^{5}I_{7}$  and  $Cr^{3+}$ :  ${}^{4}T_{2}$  to  $OH^{-}$  groups are suppressed, which is beneficial for near and mid-infrared luminescence. Based on the measured lifetimes ( $\tau_m$ ) and calculated radiative lifetimes ( $\tau_r$ ) of Ho<sup>3+</sup>:2.0 µm, the non-radiative probability  $W_{nr}$  of the  ${}^{5}I_{7}$  level can be obtained by  $W_{nr} = 1/$ 



**Fig. 8.** The average luminescent lifetime of  $Cr^{3+}$ .<sup>4</sup> $T_2$  monitored at 878 nm upon excitation of 619 nm as well as the related energy transfer efficiency  $\eta$  from  $Cr^{3+}$  to  $Ho^{3+}$ .

 $\tau_m - 1/\tau_r$  [26], the calculated results are provided at Table 7. The  $W_{nr}$  of the <sup>5</sup>I<sub>7</sub> level in fluorozirconate glass (ZBLAN) is quite low [37] due to its low maximum phonon energy and low OH<sup>-</sup> coefficient. And after 20% BaF<sub>2</sub> is added, the  $W_{nr}$  of the germanate glass is lower than that of silicate glass (359 s<sup>-1</sup>) [38]. The constantly decreased  $W_{nr}$  indicates the diminished OH<sup>-</sup> coefficient is favor of the radiative transition of Ho<sup>3+</sup>:<sup>5</sup>I<sub>7</sub>, and thus a BaF<sub>2</sub> modified germanate glass may have promising value as a material for a laser at 2.0 µm [39].

Fig. 8 depicts the average luminescent lifetimes of  $Cr^{3+}$ :<sup>4</sup> $T_2$  state in  $Cr^{3+}$  ( $\tau_{Cr}$ ) doped and  $Cr^{3+}/Ho^{3+}$  ( $\tau_{CrHo}$ ) co-doped glasses with different BaF<sub>2</sub> contents. The average lifetimes of  $Cr^{3+}$ : <sup>4</sup> $T_2 \rightarrow ^4A_2$  (878 nm) are prolonged with the substitution of BaF<sub>2</sub> added due to lowered OH<sup>-</sup> coefficient, and the lifetime of  $Cr^{3+}$  doped sample is enhanced as long as 19.75 µs by the fluorides, which is much longer than that of alkali silicate glasses (~10 µs) [11]. The transfer efficiency ( $\eta$ ) is calculated by  $\eta = 1 - \tau_{Cr}/\tau_{CrHo}$  [40]. The achieved  $\eta$  of  $Cr^{3+} \rightarrow Ho^{3+}$  varies with BaF<sub>2</sub> contents and reaches as high as 42.5% without BaF<sub>2</sub>, which is higher than that of fluorogermanate glasses (26.2%) [7] and similar to that of Yb<sup>3+</sup> (42.6%) [41]. All results indicate the Cr<sup>3+</sup> ion could be a good sensitizer for Ho<sup>3+</sup>.

#### 4. Conclusion

In summary, an enhanced 2.0  $\mu$ m emission of  $Cr^{3+}/Ho^{3+}$  co-doped germanate glass modified by  $BaF_2$  is achieved under an 808 nm LD excitation. The addition of  $BaF_2$  can distinctly diminish the refractive index and density of glass samples, furthermore, the  $OH^-$  coefficient is reduced as low as  $1.08 \text{ cm}^{-1}$  that is responsible for the promoted emission intensity and lifetime of  $Cr^{3+}$  and  $Ho^{3+}$  activators. Attractively, the excitation spectra of  $Cr^{3+}$  can be easily tailored by the incorporation of  $BaF_2$ , which ultimately makes a higher pump efficiency for achieving an efficient energy transfer process from  $Cr^{3+}$  to  $Ho^{3+}$ . An even more rewarding result is that the energy transfer efficiency from  $Cr^{3+}$  to  $Ho^{3+}$  is improved as high as 42.5% due to the suppressed non-radiative probability of  ${}^{5}I_7$  level by the substitution of  $BaF_2$ . These results suggest that  $Cr^{3+}/Ho^{3+}$  doped germanate glass modified by  $BaF_2$  can be considered as a boosted candidate for efficient 2.0  $\mu$ m fiber lasers operated at various pump sources.

#### Acknowledgments

This work is financially supported by the National Science

Foundation of China (Grants Nos. U1601205 and 51472088). Decay lifetime measurements are supported by Z.Y. Zhao from State Key Laboratory of Silicate Materials for Architectures, Wuhan University of Technology.

#### References

- L.X. Li, W.C. Wang, C.F. Zhang, J. Yuan, B. Zhou, Q.Y. Zhang, Opt. Mater. Express 6 (2016) 2904–2914.
- [2] Z.J. Xing, S. Gao, X.Q. Liu, S.Y. Sun, C.L. Yu, L.M. Xiong, K.F. Li, M.S. Liao, J. Alloys Compd. 660 (2016) 375–381.
- [3] J.T. Fan, Y.Y. Fan, Y. Yang, D.P. Chen, L. Calveza, X.H. Zhang, L. Zhang, J. Non-Cryst. Solids 357 (2011) 2431–2434.
- [4] Y. Tian, X.F. Jing, S.Q. Xu, Spectrochim. Acta A 115 (2013) 33–38.
- [5] T. Wei, Y. Tian, C. Tian, M.Z. Cai, X.F. Jing, B.P. Li, R. Chen, J.J. Zhang, S.Q. Xu, J. Phys. Chem. A 119 (2015) 6823–6830.
- [6] J. Yuan, S.X. Shen, D.D. Chen, Q. Qian, M.Y. Peng, Q.Y. Zhang, J. Appl. Phys. 113 (2013) 173507.
  [7] F.F. Zhang, J. Yuan, Y. Liu, W.C. Wang, D.C. Yu, M.Y. Peng, Q.Y. Zhang, Opt. Mater.
- Express 4 (2014) 1404–1410. [8] W.C. Wang, J.C. Tu, W.T. Feng, G.T. Zhang, Opt. Mater Express 4 (2014) 1404–1410.
- [8] W.C. Wang, J. Yuan, D.D. Chen, J.J. Zhang, S.Q. Xu, Q.Y. Zhang, AIP Adv. 4 (2014) 107145.
- [9] W.C. Wang, Q.H. Le, Q.Y. Zhang, L. Wondraczek, J. Mater. Chem. C 5 (2017) 7969–7976.
- [10] F. Rasheed, K.P.O. Donnell, B. Henderson, D.B. Hollis, J. Phys. Condens. Matter 3 (1991) 3825–3840.
- [11] U.R. Rodriguez-Mendoza, V.D. Rodriguez, I.R. Martin, V. Lavin, J. Mendez-Ramos, P. Nunez, J. Alloys Compd. 323 (2001) 759–762.
- [12] M. Yamaga, B. Henderson, K.P.O. Donnell, Y. Gao, Phys. Rev. B 44 (1991) 4853–4861.
- [13] R. Lachheb, A. Herrmann, K. Damak, C. Rüssel, R. Maâlej, J. Lumin. 186 (2017) 152–157.
- [14] D.C. Zhou, X.M. Bai, H. Zhou, Sci. Rep. 7 (2017) 44747.
- [15] R.J. Cao, Y. Lu, Y. Tian, F.F. Huang, Y.Y. Guo, S.Q. Xu, J.J. Zhang, Sci. Rep. 6 (2016) 37873.
- [16] F.F. Huang, X.Q. Liu, Y. Zhang, L.L. Hu, D.P. Chen, Opt. Lett. 39 (2014) 5917–5920.
  [17] D.H. Li, W.B. Xu, P.W. Kuan, W.T. Li, Z.Q. Lin, X. Wang, L. Zhang, C.L. Yu, K.F. Li, L.L. Hu, Ceram. Int. 42 (2016) 10493–10497.
- [18] H. Hosono, Y. Abe, J. Am. Ceram. Soc. 72 (1989) 44-48.
- [19] J.T. Fan, B. Tang, W. Dong, Y.Y. Fan, R.H. Li, J.C. Li, D.P. Chen, L. Calveza, X.H. Zhang, L. Zhang, J. Non-Cryst. Solids 357 (2011) 1106–1109.
- [20] L. Zur, J. Janek, M. Soltys, T. Goryczka, J. Pisarska, W.A. Pisarski, J. Non-Cryst. Solids 431 (2016) 145–149.
- [21] S.Q. Zhang, M.X. Xu, X. Chen, Y.L. Zhang, L. Calvez, X.H. Zhang, Y.S. Xu, Y. Huai, Y.Q. Jin, J. Am. Ceram. Soc. 96 (2013) 2461–2466.
- [22] P.L. Higby, I.D. Aggarwal, J. Non-Cryst. Solids 163 (1993) 303-308.
- [23] Z.H. Jiang, Q.Y. Zhang, Sci. China Mater. 58 (2015) 378–425;
   Z.H. Jiang, Q.Y. Zhang, Prog. Mater. Sci. 61 (2014) 144–215.
- [24] J. Yuan, S.X. Shen, W.C. Wang, M.Y. Peng, Q.Y. Zhang, Z.H. Jiang, J. Appl. Phys. 114 (2013) 133506.
- [25] H.F. Chen, F.Z. Chen, T. Wei, Q.H. Liu, R.X. Shen, Y. Tian, Opt. Commun. 321 (2014) 183–188.
- [26] F.F. Zhang, W.J. Zhang, J. Yuan, D.D. Chen, Q. Qian, Q.Y. Zhang, AIP Adv. 4 (2014) 047101.
- [27] X. Wen, G.W. Tang, J.W. Wang, X.D. Chen, Q. Qian, Z.M. Yang, Opt. Express 23 (2015) 7722–7731.
- [28] O. Maalej, O. Taktak, B. Boulard, S. Kammoun, J. Phys. Chem. B 120 (2016) 7538–7545.
- [29] D.L. Russell, K. Holliday, M. Grinberg, D.B. Hollis, Phys. Rev. B 59 (1999) 13712–13718.
- [30] B.R. Judd, Phys. Rev. 127 (1962) 750-761.
- [31] G.S. Ofelt, J. Chem. Phys. 37 (1962) 511-520.
- [32] G.X. Chen, Q.Y. Zhang, G.F. Yang, Z.H. Jiang, J. Fluoresc. 17 (2007) 301-307.
- [33] B. Peng, T. Izumitani, Opt. Mater. 4 (1995) 797-810.
- [34] T.T. Zhu, G.W. Tang, X.D. Chen, M. Sun, Q. Qian, D.D. Chen, Z.M. Yang, Int. J. Appl. Glas. Sci. 8 (2017) 196–203.
- [35] Y. Tian, L.Y. Zhang, S.Y. Feng, R.R. Xu, L.L. Hu, J.J. Zhang, Opt. Mater. 32 (2010) 1508–1513.
- [36] T. Wang, F.F. Huang, W.Q. Cao, Y.Y. Guo, R.S. Lei, R.G. Ye, J.J. Zhang, S.Q. Xu, Opt. Mater. Express 7 (2017) 1084–1095.
- [37] L. Wetenkamp, G.F. West, H. Többen, J. Non-Cryst. Solids 140 (1992) 35-40.
- [38] X. Wang, X.K. Fan, S. Gao, K.F. Li, L.L. Hu, Ceram. Int. 40 (2014) 9751–9756.
- [39] R. Reisfeld, J. Hormadaly, A. Muranevich, J. Non-Cryst. Solids 29 (1978) 323–332.
  [40] W.C. Wang, J. Yuan, X.Y. Liu, D.D. Chen, Q.Y. Zhang, Z.H. Jiang, J. Non-Cryst.
- Solids 404 (2014) 19–25. [41] L.L. Tao, Y.H. Tsang, B. Zhou, B. Richards, A. Jha, J. Non-Cryst. Solids 358 (2012)
- 1644–1648.