

Contents lists available at ScienceDirect

Journal of Luminescence



journal homepage: www.elsevier.com/locate/jlumin

Judd–Ofelt analysis and stimulated-emission cross-sections for highly doped (38 at%) Er:YSGG laser crystal



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ARTICLE INFO

Article history: Received 31 May 2015 Received in revised form 24 October 2015 Accepted 27 October 2015 Available online 2 December 2015

Keywords: Erbium ions Gallium garnets Judd–Ofelt analysis Stimulated emission

ABSTRACT

Stimulated-emission cross-section spectra are determined for the \sim 1.5 μ m and 3 μ m transitions of Er^{3+} ions in YSGG crystal. For the ${}^{4}I_{13/2} \rightarrow {}^{4}I_{13/2}$ channel, the maximum stimulated-emission cross-section σ_{SE} is 0.43 \times 10⁻²⁰ cm² at 2797.1 nm. For the ${}^{4}I_{13/2} \rightarrow {}^{4}I_{15/2}$ channel, σ_{SE} =1.20 \times 10⁻²⁰ cm² at 1532.8 nm. Due to the reabsorption loss, laser operation is expected at \sim 1644 nm. Radiative lifetimes of all excited states of the Er^{3+} ion from {}^{4}I_{13/2} or ${}^{2}H_{9/2}$ and probabilities of radiative transitions from these states are determined using the Judd–Ofelt theory. Radiative lifetimes of the {}^{4}I_{13/2} and {}^{4}I_{11/2} excited states for Er^{3+} ions in YSGG are 7.73 ms and 9.75 ms, respectively. Non-radiative decay is analyzed for lower excited-states of Er^{3+} ions in YSGG.

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1. Introduction

Erbium-doped garnets are widely used as laser crystals for the generation of ~1.5 and 3 µm radiation [1–4]. The 3 µm transition of Erbium doped lasers falls at a peak in the water absorption spectrum making laser sources at this wavelength extremely useful in medicine and dentistry [5,6]. A difficulty associated with this laser transition is that the lower laser level (⁴I_{13/2}) has a longer lifetime than the upper laser level (⁴I_{11/2}), which would usually result in self terminating behavior [7–10]. However, with highly doped Erbium crystals this effect can be counteracted via energy transfer upconversion (ETU) processes which recycle population from the lower laser level back to the upper laser level (and are stronger at higher doping levels when the $\text{Er}^{3+}-\text{Er}^{3+}$ inter-ionic distance is less) [7–10]. This mechanism is shown in Fig. 1 (labeled W₁₁) which is an energy level diagram for the system.

For successful laser construction and theoretical modeling of $\sim 3 \,\mu m$ laser systems it is necessary to have accurate spectroscopic data on highly doped Erbium crystals. The majority of $3 \,\mu m$ laser studies on Erbium doped garnets has been undertaken using Er: YAG, but an interesting competitor for this material is Er:

Y₃Sc₂Ga₃O₁₂ (Er:YSGG) [11,12]. This crystal has a significantly longer upper laser level lifetime for the ~3 µm transition, ⁴I_{11/2}, compared to Er:YAG (1.3 ms vs. 120 µs [2]), providing better energy storage potential which could translate into superior Qswitched performance. Moreover the shorter lower laser level lifetime of Er:YSGG compared to Er:YAG [2] could prove advantageous in reducing the likelihood of self-termination of the 3 µm transition. Spectroscopic properties of Er,Cr:YSGG were studied in Refs. [13,14]. Previous papers on Er:YSGG focused on structure of energy-levels of Er³⁺ ions [15], Judd–Ofelt modeling [16,17] and up- conversion luminescence [18,19]. However, some relevant spectroscopic parameters of the Er:YSGG material are still not well known, specifically the stimulated emission cross section for both the ~1.5 and 3 µm transition.

In this work, a detailed spectroscopic study of a highly doped 38 at% Er:YSGG crystal is undertaken. Absorption and luminescence spectra are presented and stimulated emission cross sections are calculated for the \sim 1.5 and 3 μm laser transitions. The radiative lifetimes of the relevant excited states of the Erbium system are calculated using the conventional Judd–Ofelt (J–O) theory. Furthermore, the luminescence branching ratios, absorption oscillator strengths and probabilities of spontaneous radiative transitions are determined.

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2. Experimental

The studied crystal was $Y_3Sc_2Ga_3O_{12}$ (YSGG) doped with 38 at% Er. The Er concentration, $N_{\rm Er}$, determined with Electron Probe MicroAnalysis (EPMA) was 48.2×10^{20} at/cm³. Such a high Er content was selected as it corresponded to the typical doping levels (30...50 at%) for Er:YSGG active elements used in ~3 µm lasers reported so far [2,11,12]. In addition, we aimed to study the influence of high doping level on the spectroscopic parameters of Er³⁺ ions. Indeed, as the ionic radius of six-fold oxygen-coordinated Y³⁺ ion (0.90 Å) is slightly larger than that of Er³⁺ ion (0.89 Å), high-level crystal doping can induce slight variation of the crystal structure and, hence, f-f transition intensities. For



Fig. 1. Erbium energy level diagram.

instance, this effect was observed for 0.5–29 at% Er-doped YAG crystals [20].

Optical absorption spectra of Er:YSGG were measured with a Varian CARY 5000 spectrophotometer at room-temperature (RT, \sim 293 K). The spectral bandwidth (SBW) was \sim 0.02 nm. To avoid saturation of the detector, the sample used for absorption measurements was a thin (thickness: 100 µm) polished plate.

Photoluminescence (PL) of Er^{3+} ions was excited by the focused output of a 962 nm InGaAs laser diode (the maximum power density on the sample was $\sim 1 \, \mathrm{kW/cm^2}$). The PL was collected in the direction perpendicular to the excitation direction by a wide-aperture lens. The spectrum was registered by means of a lock-in amplifier, monochromator MDR-23 (SBW $\sim 0.2 \, \mathrm{nm}$) and sensitive Hamamatsu C5460-01 (0.4–0.9 $\mu \mathrm{m}$) and G5851 (0.9–1.7 $\mu \mathrm{m}$) photodetectors. The monochomator was calibrated with Xe lamp. The emission of the Er^{3+} ions at $\sim 3 \, \mu \mathrm{m}$ was detected with a compact Fourier transform infrared spectrometer, FT-IR Rocket from Arcoptix. As an excitation source, Ti:Sapphire laser tuned to $\sim 962 \, \mathrm{nm}$ was used.

For the luminescence decay measurements, an optical parametric oscillator Lotis TII LT-2214 tuned to 545, 650, 800, 960 or 1480 nm was used as the excitation source; the duration of the excitation pulse was \sim 20 ns. The PL was collected by a wideaperture lens and re-imaged to the input slit of the monochromator MDR-12 (SBW \sim 1 nm), before detection by a fast Hamamatsu C5460 or G5851 photodetector (response time, 40 ns) and 500 MHz Textronix TDS-3052B digital oscilloscope.

3. Results and discussion

The absorption spectrum of the Er:YSGG crystal is shown in Fig. 2. The absorption band related to the ${}^{4}I_{15/2} \rightarrow {}^{4}I_{11/2}$ transition, used for pumping of Er:YSGG crystals with InGaAs laser diodes, contains three intense peaks centered at 962.5, 965.8 and 968.8 nm. The corresponding absorption cross-section, σ_{abs} , is $\sim 0.46 \times 10^{-20} \text{ cm}^2$. Full



Fig. 2. Absorption cross-section spectra for 38 at% Er:YSGG crystal.

width at half maximum (FWHM) for these peaks is relatively small, < 1.5 nm. For the band related to the ${}^{4}I_{15/2} \rightarrow {}^{4}I_{13/2}$ transition, typically used for the resonant (inband) pumping of Er^{3+} lasers, the maximum σ_{abs} value is $1.02 \times 10^{-20} \text{ cm}^2$ at 1532.6 nm. The spectral features determined for 38 at% Er:YSGG crystal are similar to one reported in Refs. [16,17] for the same crystal with a lower Er doping level.

Absorption oscillator strengths for Er^{3+} ions were calculated directly from the measured absorption spectrum $\alpha(\lambda)$:

$$f_{\exp} = \frac{m_{\rm e}c^2}{\pi e^2 N_{\rm Er}\overline{\lambda}^2} \int \alpha(\lambda) d\lambda \tag{1}$$

where $\bar{\lambda}$ is the coordinate of a "center of gravity" of the selected absorption band (mean wavelength), $N_{\rm Er}$ is the concentration of ${\rm Er}^{3+}$ ions, $m_{\rm e}$ and e are the electron mass and charge, respectively; the integration is performed over the absorption band.

In addition, absorption oscillator strengths were calculated from the line strength *S*(JJ') modeled within the conventional Judd–Ofelt (J–O) theory [21,22]:

$$S_{\rm ED}(JJ') = \sum_{k} e^2 \Omega_k | \langle \gamma J | U^k | \gamma' J' \rangle |^2$$
⁽²⁾

Here, the summation is performed for $k=2, 4, 6; |<\gamma J|U^{k_1}$ $\gamma' J' > |^2$ is the square of reduced matrix element of the unit matrix U^k , E_J and E_J' are the energies of γJ and $\gamma' J'$ multiplets, { Ω_2, Ω_4 and Ω_6 } are the intensity (J–O) parameters. An expression for the calculation of *f* values from the corresponding line strengths is:

$$f_{\rm ED} = \frac{8\pi^2 m_e c}{3(2J+1)\overline{\lambda}he^2} \frac{(n^2+2)^2}{9n} S_{\rm ED}(JJ')$$
(3)

where *n* is the crystal refractive index [23] at the wavelength of $\overline{\lambda}$. J–O theory allows for a calculation of the line strengths for electricdipole (ED) transitions. The contribution of magnetic-dipole (MD) transitions with J–J'=0, ± 1 was calculated separately using the Russell–Saunders approximation on wave functions of Er³⁺ ions under the assumption of a free-ion. Total calculated oscillator strengths were then $f_{calc}=f_{ED}+f_{MD}$. Prior to the fitting of experimental oscillator strengths with the J–O model, MD contributions were subtracted from the f_{exp} values.

The wave functions in the intermediate coupling scheme (ICS) corresponding to the states (energy levels) of the rare-earth ions are linear combinations of wave functions in the Russell–Saunders approximation (the L–S coupling scheme). The energy levels are designated usually by means of one or more L–S wave functions which contribute mainly to this linear combination. For designating of high-lying excited-states of Er^{3+} (see Fig. 1), we used this system. This means that the L–S wave functions ($^{2}\text{G}, ^{4}\text{F}, ^{2}\text{H})_{9/2}$, ($^{2}\text{P}, ^{2}\text{P}, ^{4}\text{F})_{3/2}$ and ($^{2}\text{H}, ^{2}\text{G})_{9/2}$ contribute mainly to the ICS wave function of Er^{3+} with energy level of ~24,550 cm⁻¹, 31,600 cm⁻¹ and 36,550 cm⁻¹, respectively.

Results on the experimental and calculated absorption oscillator strengths of Er³⁺ ions are presented in Table 1. For J–O theory, the obtained parameters are Ω_2 =2.22, Ω_4 =1.50 and Ω_6 =0.46 $[10^{-20} \text{ cm}^2]$. In Table 2, we compared obtained I–O parameters with the ones reported previously for Er:YSGG [16,17] and different Er-doped crystals [24-28]. In addition, spectroscopy quality factors, $X_{2/6} = \Omega_2 / \Omega_6$ and $X_{4/6} = \Omega_4 / \Omega_6$, introduced by Kaminski [24], are calculated. They are used to estimate the potential of active materials for laser operation as they are linked to the luminescence branching ratios. For Er:YSGG, $X_{2/6}=4.82$ and $X_{4/6}$ = 3.26 that agrees with the range determined by Kaminski [24], Table 2. J–O parameters obtained in the present paper for 38 at% Er:YSGG are different from the ones reported by Su et al. for 30 at% Er:YSGG [16], $\Omega_2=0.23$, $\Omega_4=0.86$ and $\Omega_6=0.37$ and by Sardar et al. for 1 at% Er:YSGG [17], $\Omega_2{=}0.92$, $\Omega_4{=}0.48$ and $\Omega_6=0.87~[10^{-20}~{
m cm}^2]$. This is partially referred to the difference in

Table 1

Absorption oscillator strengths f_{exp} [determined from the absorption spectra, Eq. (1)], f_{calc} (calculated by means of J–O theory) and integrated absorption coefficient Γ for Er³⁺ ion in the YSGG crystal.

${}^{4}\!I_{15/2}\!\rightarrow$	Wavenumbers, cm ⁻¹	<i>Г</i> , nm•cm ⁻¹	Absorption oscillator strengths [*] , 10 ⁻⁶		
			$f_{\rm exp}$	f_{calc}	
⁴ I _{13/2}	6278-6592	697.6	0.676	$0.647^{ed} + 0.564^{md}$	
${}^{4}I_{11/2}$	10,188- 10,389	177.1	0.439	0.254	
⁴ I _{9/2}	12,310- 12,731	79.5	0.290	0.378	
⁴ F _{9/2}	15,223- 15,460	287.9	1.588	1.768	
${}^{4}S_{3/2}$	18,371- 18,474	44.3	0.352	0.213	
$^{2}H_{11/2}$	19,035- 19,436	342.9	2.972	3.348	
${}^{4}F_{7/2}$	20,457-20,640	123.9	1.226	1.188	
⁴ F _{5/2}	22,254-22,508	36.3	0.419	0.258	
${}^{4}F_{3/2}$	22,583-22,646	26.4	0.317	0.151	
(² G, ⁴ F, ² H) _{9/2}	24,367- 24,773	42.1	0.595	0.371	
${}^{4}G_{11/2}$	26,151-26,643	375.3	6.127	5.921	
${}^{4}G_{7/2} + {}^{4}G_{9/2}$	27,254- 28,148	114.8	2.063	$1.784^{ed} + 0.067^{md}$	
$({}^{2}P, {}^{2}D, {}^{4}F)_{3/2}$	31,439- 31,579	3.6	0.084	0.029	
² K _{13/2}	33,093- 33,676	11.6	0.303	0.060	
${}^{4}G_{5/2} + {}^{2}P_{1/2}$	-				
${}^{4}G_{7/2}$	33,950- 34,150	6.2	0.168	0.201	
$^{2}D_{5/2}$	34,728- 34,894	3.1	0.088	0.042	
$({}^{2}H, {}^{2}G)_{9/2}$	36,279- 36,514	17.9	0.556	0.312	
rms dev.	, , ,,,			0.245	

* Superscripts ED and MD represent contribution of electric-dipole and magnetic-dipole transitions, respectively. Numbers without superscripts correspond to pure ED transitions.

Table 2

Judd–Ofelt parameters Ω_k (k=2, 4, 6) and spectroscopic quality factors $X_{2/6}=\Omega_2/\Omega_6$ and $X_{4/6}=\Omega_4/\Omega_6$ for various Er^{3+} -doped crystals.

Crystal	Judd–Ofel $(k=2, 4, 6)$	lt paramete 6), 10 ⁻²⁰ ci	ers, Ω _k m²	Spectroscopic quality factors		Ref.	
	Ω_2	Ω_4	Ω_6	X _{2/6}	X _{4/6}		
Er:YSGG Er:GGG	2.22 0.23 0.92 0.70	1.50 0.86 0.48 0.37	0.46 0.37 0.87 0.86	4.82 0.62 1.06 0.81	3.26 1.62 0.55 0.43	This work [16] [17] [17]	
Er:YAG Er:LuAG Er:CNGG Er:GSGG Er:Y ₂ O ₃ Er:YAlO ₃	0.47 0.47 3.74 0.35 4.59 0.95	0.96 1.04 3.15 2.35 1.21 0.58	0.61 0.7 2.58 3.23 0.48 0.55	0.52-8.9* 0.60-11.4* 1.45 0.11 9.56 1.72	1.57-2.11* 1.47-2.11* 1.22 0.73 2.52 1.05	[24] [24] [25] [26] [27] [28]	

* Taking into account hyper-sensitive Er³⁺ transitions.

Er concentration. Indeed, J–O parameters are sensitive to the intensities of hypersensitive Er^{3+} transitions [24] which are in turn affected by the crystal field.

It is well known that the excited configurations can affect the Stark splitting of the multiplets [29] as well as transition intensities [30]. These configurations have different influence on the lower and higher lying multiplets. This is mainly related to the energy gap between the multiplet and excited configuration. Within the J–O theory, excited configurations are considered to be completely degenerated and thus the above mentioned influence is not taken into account. The use of J–O theory for the description of transition intensities for Er^{3+} doped materials is typically successful [24–28]. This is due to the fact that multiplets of Er^{3+} ion are strongly "mixed" by the crystalline field and the difference in the action of excited configurations on different multiplets is near negligible. Indeed, the J–O theory allowed us to obtain low rootmean-square (rms) deviation between the experimental and calculated *f* values (rms dev.=0.245).



Fig. 3. (a) Near-IR luminescence from 38 at% Er:YSGG crystal, bands at 0.95–1.7 μ m and 2.6–3 μ m are not in scale and (b) up-conversion luminescence (UCL) from this crystal, excitation wavelength is 962 nm.

PL spectra of the Er:YSGG crystal are shown in Fig. 3 (for excitation to the ${}^{4}I_{11/2}$ state by 962 nm radiation). Near-IR emissions at 0.95–1.05, 1.45–1.66 and 2.6–2.95 µm correspond to the transitions ${}^{4}I_{11/2} \rightarrow {}^{4}I_{15/2}$, ${}^{4}I_{13/2} \rightarrow {}^{4}I_{15/2}$ and ${}^{4}I_{11/2} \rightarrow {}^{4}I_{13/2}$, respectively. All visible emissions are due to up-conversion luminescence (UCL). The red emission band spanning from 640 to 690 nm and related to the transition ${}^{4}F_{9/2} \rightarrow {}^{4}I_{15/2}$ dominates in this spectrum. Green UCL (510–570 nm) from the closely located and thermalized states, ${}^{2}H_{11/2}$ and ${}^{4}S_{3/2}$, is much weaker. The ratio of the integrated intensities of these bands (R/G) is 3.1. Near-IR UCL at 780–870 nm is due to the ${}^{4}I_{9/2} \rightarrow {}^{4}I_{15/2}$ and ${}^{4}S_{3/2} \rightarrow {}^{4}I_{13/2}$ transitions. In the blueviolet region, very weak emissions at ~415 and 450 nm occur from the higher-lying ${}^{2}H_{9/2}$ and ${}^{4}F_{3/2} + {}^{4}F_{5/2}$ excited states, respectively.

In Fig. 4, log-log plots for the UCL intensity, I_{UCL}, vs. the excitation power density W are shown. UCL is a non-linear process, so typically $I_{\text{UCI}} \sim W^n$ (the so-called power law). The parameter n indicates the number of pump photons involved in the UCL mechanism. On a log-log scale, n corresponds to the slope of the above mentioned dependence. First we consider the case of low power densities ($< 0.2 \text{ kW/cm}^2$). For green emissions that occur from the ${}^{2}H_{11/2}$ and ${}^{4}S_{3/2}$ states, n = 1.8 (542 nm) and 2.0 (557 nm) which means that two pump photons are required to populate the above mentioned states. A pump wavelength of \sim 962 nm corresponds to the ground-state absorption (GSA) ${}^{4}I_{15/2} \rightarrow {}^{4}I_{11/2}$. Further excitation is typically due to an excited state absorption (ESA) ${}^{4}I_{11/2} \rightarrow {}^{4}F_{7/2}$ or energy-transfer up-conversion (ETU) for adjacent Er^{3+} ions, ${}^{4}I_{11/2} + {}^{4}I_{11/2} \rightarrow {}^{4}I_{15/2} + {}^{4}F_{7/2}$. Taking into account fast non-radiative relaxation from the ${}^{4}F_{7/2}$ state, both ${}^{2}H_{11/2}$ and ${}^{4}S_{3/2}$ states are normally populated in a scheme that requires 2 pump photons that is in agreement with Fig. 4(a). For near-IR UCL at 857 nm, also occurring from the ${}^{4}S_{3/2}$ state, n=1.9.

For red emission at 672 nm, n=2.0. Population of the ${}^{4}F_{9/2}$ state, which is responsible for this emission, normally occurs in three steps. These are GSA, followed by a non-radiative relaxation to the intermediate ${}^{4}I_{13/2}$ level and second intense ESA channel ${}^{4}I_{13/2} \rightarrow {}^{4}F_{9/2}$. For crystals with a high Er content like in our case, there is an additional mechanism that allows for further enhancement of the excitation efficiency, namely cross-relaxation (CR). First intense CR scheme is ${}^{4}F_{7/2} + {}^{4}I_{15/2} \rightarrow {}^{4}F_{9/2} + {}^{4}I_{13/2}$ that raises red UCL. Second relevant CR scheme is ${}^{4}S_{3/2}, {}^{2}H_{11/2} + {}^{4}I_{15/2} \rightarrow {}^{4}I_{9/2} + {}^{4}I_{13/2}$ that depopulates thermalized ${}^{4}S_{3/2}, {}^{2}H_{11/2}$ states responsible for green emission. Increase of Er doping leads to a decrease of average inter-ionic distances and, hence, to a fast enhancement of the CR efficiency. In contrast, ESA



Fig. 4. Dependence of the UCL intensity on the excitation power density for 38 at% Er:YSGG, *points* are the experimental data, *lines* are their fitting for the slope (*n*) calculation.

process is not significantly affected by Er doping level. Thus, red UCL is enhanced much stronger as compared with the green UCL from the thermalized ${}^{2}H_{11/2}$ + ${}^{4}S_{3/2}$ states that results in R/G ratio being > 1 for highly Er-doped crystals. Indeed, for 38 at. % Er:YSGG, R/G=3.1 as mentioned above.

The reduced value of *n* for red UCL at high excitation power densities $> 0.2 \text{ kW/cm}^2$ ($n \sim 1.1$) is related to the competition of a linear decay (near-IR luminescence around 1.54 µm from the ${}^{4}I_{13/2}$ state) and upconversion itself (due to ESA from the ${}^{4}I_{13/2}$ state) in the depletion of the intermediate excited state, ${}^{4}I_{13/2}$. It was shown [31] that for strong UCL, *n* is typically < 2 and can even approach 1. This prediction agrees with our results shown in Fig. 4. Similar behavior is observed for green and near-IR UCL.

Using the parameters presented in Table 2, we calculated line strengths $S_{ED}(JJ')$ for spontaneous radiative transitions from all excited states of the Er^{3+} ion from ${}^{4}I_{13/2}$ to ${}^{2}H_{9/2}$. On the basis of $S_{ED}(JJ')$ values, the corresponding probabilities of these transitions $A_{ED}(JJ')$ were determined as:

$$A_{\rm ED}(JJ') = \frac{64\pi^4}{3h(2J+1)\overline{\lambda}^3} n(\frac{n^2+2}{3})^2 S_{\rm ED}(JJ') \tag{4}$$

The total probabilities, $A(JJ')=A_{ED}(JJ')+A_{MD}(JJ')$, were then determined by adding MD contributions determined separately. Radiative lifetimes of the excited-states τ_{rad} and luminescence branching ratios B(JJ') were then determined as:

$$\tau_{\rm rad} = \frac{1}{\sum_{J'} A(JJ')}$$
(5a)

$$B(JJ') = \frac{A(JJ')}{\sum_{l'} A(JJ')}$$
(5b)

Luminescence branching ratios B(JJ') for spontaneous radiative transitions from the ${}^{4}I_{13/2}...{}^{2}H_{9/2}$ states of Er^{3+} ions in YSGG determined with the J–O theory are shown in Table 3. For transitions from the ${}^{4}I_{11/2}$ state that is the upper-laser level for $\sim 3 \,\mu\text{m}$ Erbium lasers, $B({}^{4}I_{11/2} \rightarrow {}^{4}I_{15/2}) = 74.6\%$ and $B({}^{4}I_{11/2} \rightarrow {}^{4}I_{13/2}) = 25.4\%$. In Table 4, we compared these values with the ones reported previously for Er:YSGG and different well-known Er-doped laser materials. The values calculated by us agree well with the ones reported for 30 at% Er:YSGG in [16], namely 72.6% and 27.4\%, respectively. They are also in agreement with ones presented for cubic garnets, Er:YAG, LuAG [24], GGG and GSGG [32].

Radiative lifetimes τ_{rad} for the ${}^{4}I_{13/2}...{}^{2}H_{9/2}$ excited-states of Er³⁺ ions in YSGG crystal are summarized in Table 5. Relatively good agreement of all τ_{rad} values is observed with the previous report for 30 at% Er:YSGG [16]. For ${}^{4}I_{13/2}$ and ${}^{4}I_{11/2}$ states which are interesting for laser applications, τ_{rad} is 7.73 and 9.75 ms,

Table 3 Luminescence branching ratios B(JJ') for Er^{3+} ions in YSGG calculated with the Judd–Ofelt theory.

Initial state	Final state	B(JJ')	Initial state	Final state	B(JJ')
⁴ I _{13/2}	⁴ I _{15/2}	1.0	${}^{4}F_{5/2}$	$^{4}I_{15/2}$	0.345
${}^{4}I_{11/2}$	⁴ I _{15/2}	0.746	3/2	⁴ I _{13/2}	0.488
/-	⁴ I _{13/2}	0.254		⁴ I _{11/2}	0.075
⁴ I _{9/2}	⁴ I _{15/2}	0.868		⁴ I _{9/2}	0.039
-,-	⁴ I _{13/2}	0.120		⁴ F _{9/2}	0.051
	$^{4}I_{11/2}$	0.012		${}^{4}S_{3/2}$	< 0.001
⁴ F _{9/2}	⁴ I _{15/2}	0.923		$^{2}H_{11/2}$	0.001
.,	⁴ I _{13/2}	0.046		⁴ F _{7/2}	< 0.001
	$^{4}I_{11/2}$	0.028	⁴ F _{3/2}	⁴ I _{15/2}	0.371
	⁴ I _{9/2}	0.003	,	⁴ I _{13/2}	0.036
⁴ S _{3/2}	$4I_{15/2}$	0.660		$^{4}I_{11/2}$	0.372
	⁴ I _{13/2}	0.270		⁴ I _{9/2}	0.207
	${}^{4}I_{11/2}$	0.022		⁴ F _{9/2}	0.007
	⁴ I _{9/2}	0.048		${}^{4}S_{3/2}$	0.007
	${}^{4}F_{9/2}$	< 0.001		$^{2}H_{11/2}$	< 0.001
² H _{11/2}	$4I_{15/2}$	0.917		${}^{4}F_{7/2}$	< 0.001
	${}^{4}I_{13/2}$	0.050		${}^{4}F_{5/2}$	< 0.001
	${}^{4}I_{11/2}$	0.019	(² G, ⁴ F, ² H) _{9/2}	$4I_{15/2}$	0.346
	⁴ I _{9/2}	0.012		⁴ I _{13/2}	0.448
	⁴ F _{9/2}	0.003		⁴ I _{11/2}	0.141
	⁴ S _{3/2}	< 0.001		⁴ I _{9/2}	0.010
⁴ F _{7/2}	⁴ I _{15/2}	0.674		⁴ F _{9/2}	0.040
	⁴ I _{13/2}	0.208		⁴ S _{3/2}	< 0.001
	${}^{4}I_{11/2}$	0.077		$^{2}H_{11/2}$	0.010
	⁴ I _{9/2}	0.033		⁴ F _{7/2}	0.003
	⁴ F _{9/2}	0.007		⁴ F _{5/2}	< 0.001
	⁴ S _{3/2}	< 0.001		⁴ F _{3/2}	< 0.001
	$^{2}H_{11/2}$	< 0.001			

Table 4

Luminescence branching ratios B(JJ') from the ${}^4I_{11/2}$ excited-state for Er^{3+} ions in various crystals.

Crystal	$B({}^{4}I_{11/2} \rightarrow {}^{4}I_{15/2})$	$B({}^{4}I_{11/2} \rightarrow {}^{4}I_{13/2})$	Ref.
Er:YSGG	74.6%	25.4%	This work
	72.6%	27.4%	[16]
	88.7%	11.3%	[17]
Er:GGG	88.8%	11.2%	[17]
	78%	22%	[32]
Er:GSGG	77%	23%	[32]
Er:YAG	80.2%	19.8%	[24]
Er:LuAG	81.2%	18.8%	[24]
Er:Y ₂ O ₃	81.3%	18.7%	[27]
Er:KY ₃ F ₁₀	73%	27%	[32]

Table 5			
Lifetimes of the excited-states	for	Er:YSGG	crvstal*.

Excited state	Er:YSGG/calculated			Er:YSGG/measured	
	This work τ _{rad} , μs	Ref. [16] τ _{rad} , μs	Ref. [17] τ _{rad} , μs	This work τ _{exp} , μs	Ref. [2] τ _{exp} , μs
⁴ I _{13/2}	7731	6615	7919	2235	3400
$^{4}I_{11/2}$	9747	8868	5652	1300	1300
⁴ I _{9/2}	4270	5706	6998	0.35	-
⁴ F _{9/2}	653	812	778	10.2	-
${}^{4}S_{3/2}$	1078	874	437	0.4	-
$^{2}H_{11/2}$	261	538	326	0.4	-
⁴ F _{7/2}	316	336	250	-	-
${}^{4}F_{5/2}$	484	464	378	-	-
${}^{4}F_{3/2}$	562	521	-	-	-
(² G, ⁴ F, ² H) _{9/2}	448	1711	-	-	-
⁴ G _{11/2}	71	-	-	-	-

* τ_{rad} – radiative lifetimes calculated with the Judd–Ofelt theory; τ_{exp} – lifetime determined from the PL decay.

Table 6

Radiative lifetimes τ_{rad} of the ${}^4I_{13/2}$ and ${}^4I_{11/2}$ excited-states for $Er^{3\,+}$ ions in various crystals.

Crystal	$\tau_{\rm rad}({}^{4}{\rm I}_{13/2})$, ms	$\tau_{\rm rad}(^4 {\rm I}_{11/2})$, ms	Ref.
Er:YSGG Er:GGG Er:YAG Er:LuAG Er:Y ₂ O ₃ Er:LaF ₂	7.73 7.64 7.3 6.8 7.75 10.9	9.75 5.48 8.8 7.8 6.81 11.6	This work [17] [24] [24] [27] [33]
Er:YLF	10.0	6.7	[34]

respectively (as determined with the J–O theory). This is close to the result of [16] also obtained with the J–O theory, namely 6.62 and 8.87 ms, respectively. In Table 6, we compared radiative lifetimes of the ⁴I_{13/2} and ⁴I_{11/2} states for different Er³⁺-doped crystals reported so far. A relatively good agreement of results for the ⁴I_{13/2} state is observed. In contrast, for the ⁴I_{11/2} state, the value of τ_{rad} for the Er:YSGG crystal is longer than ones determined for cubic Er-doped garnets (5–8 ms) [17,24] that highlights its potential for 3 µm laser operation.

The knowledge of radiative lifetimes τ_{rad} for the ${}^{4}I_{13/2}$ and ${}^{4}I_{11/2}$ states allows for determination of stimulated-emission crosssections, σ_{SE} , for laser-active transitions ${}^{4}I_{13/2} \rightarrow {}^{4}I_{15/2}$ (lasing at $\sim 1.5 \ \mu$ m) and ${}^{4}I_{11/2} \rightarrow {}^{4}I_{13/2}$ (at $\sim 3 \ \mu$ m). In both cases, the Füchtbauer–Ladenburg (F–L) equation [35] was used:

$$\sigma_{\rm SE}(\lambda) = \frac{\lambda^5}{8\pi n^2 \tau_{\rm rad} c} \frac{3W(\lambda)}{\int \lambda W(\lambda) d\lambda}$$
(6)

Here $W(\lambda)$ is the measured spectral power density of luminescence. In addition, for the ${}^{4}I_{13/2} \rightarrow {}^{4}I_{15/2}$ transition, we used the reciprocity method:

$$\sigma_{\rm SE}(\lambda) = \sigma_{\rm abs}(\lambda) \frac{Z_1}{Z_2} \exp\left(-\frac{hc/\lambda - E_{\rm ZL}}{kT}\right)$$
(7)

where Z_1 and Z_2 are the lower and upper manifold partition functions, respectively, E_{ZL} is the energy corresponding to the zero phonon line, k is the Boltzmann constant and T is the crystal temperature (room-temperature). Partition functions are determined as:

$$Z_m = \sum_k g_k^m \exp(-E_k^m / kT)$$
(8)

where m=1, 2; g_k^m is the degeneration of the sublevel having the number k and the energy E_k^m measured from the lower sublevel of the corresponding multiplet. The energies of sublevels for the ${}^4I_{13/2}$ and ${}^4I_{15/2}$ multiplets for Er:YSGG crystal were taken from [15]. Calculation of σ_{SE} with the reciprocity method is beneficial as it does not require the information about the radiative lifetime τ_{rad} of the emitting state as well as direct measurement of the emission spectrum that can be affected by the reabsorption loss. There exists third possibility for the calculation of σ_{SE} values, the so-called modified reciprocity method [36]:

$$\sigma_{\rm SE}(\lambda) = \frac{3\exp(-hc/(kT\lambda))}{8\pi n^2 \tau_{\rm rad} c \int \lambda^{-4} \sigma_{\rm abs}(\lambda) \exp(-hc/(kT\lambda)) d\lambda} \sigma_{\rm abs}(\lambda) \tag{9}$$

Modified reciprocity method does not refer to the emission spectrum $W(\lambda)$ but it requires the data about $\tau_{\rm rad}$ value. Thus, a simultaneous use of Eqs. (7) and (9) can result in an estimation of the radiative lifetime of the emitting state that is the ${}^{4}I_{13/2}$ state in our case.

The results for σ_{SE} are shown in Fig. 5. For the ${}^{4}I_{13/2} \rightarrow {}^{4}I_{15/2}$ transition, the use of reciprocity method corresponds to a better resolution of spectral features as compared with the F–L equation, partially referred to a better spectral resolution used in the



Fig. 5. Stimulated-emission cross-section σ_{SE} spectra for the ${}^{4l}_{1_{1/2}} \rightarrow {}^{4l}_{1_{5/2}}$ (a) and ${}^{4l}_{1_{1/2}} \rightarrow {}^{4l}_{1_{3/2}}$ (c) transitions of Er³⁺ ions in Er:YSGG crystal, as calculated with the reciprocity, Eq. (7) and Füchtbauer–Ladenburg (F–L) methods, Eq. (6); gain cross-section, $\sigma_{g} = \beta \sigma_{SE} - (1 - \beta) \sigma_{abs}$, spectrum for the ${}^{4l}_{1_{3/2}} \rightarrow {}^{4l}_{1_{5/2}}$ transition (b), β is the inversion ratio.

absorption measurements and partially to the reabsorption losses that are strong for highly doped 38 at% Er:YSGG crystals. The maximum stimulated-emission cross-section σ_{SE} is $1.20 \times 10^{-20} \, \text{cm}^2$ at 1532.8 nm. Estimation of the radiative lifetime $\tau_{\rm rad}$ of the ${}^{4}I_{13/2}$ state with the modified reciprocity method yields the value of 5.5 \pm 0.5 ms that is shorter than one determined from the J-O modeling, 7.73 ms. This effect was previously observed in Ref. [32]. It can be explained as following. In the J-O theory, it is assumed that all the crystal field levels of each multiplet are equally populated. For the case of Er:YSGG crystal, the ⁴I_{15/2} ground state is split into two groups of four levels separated by \sim 400 cm⁻¹ [15]. Thus, the transitions from the four lower ${}^{4}I_{15/2}$ sub-levels to the ${}^{4}I_{11/2}$ and ${}^{4}I_{13/2}$ states are much stronger than they are from the upper four sub-levels. Since the lower group of levels is predominantly populated at room temperature, this splitting leads to an enhancement of the observed oscillator strength and therefore slight underestimate of the Judd-Ofelt radiative lifetime.

For laser applications, a useful parameter is also the gain crosssection, σ_g :

$$\sigma_{\rm g}(\lambda) = \beta \sigma_{\rm SE}(\lambda) - (1 - \beta) \sigma_{\rm abs}(\lambda) \tag{10}$$

where β is the inversion ratio, $\beta = N_2/N_0$ where N_2 and N_0 are the numbers of ions in the upper laser level and overall number of ions, respectively. The gain spectra for the Er:YSGG crystal for $\beta < 0.5$ are shown in Fig. 5(b). In accordance with this plot, the dominant wavelength in the Er:YSGG laser working on the ${}^{4}I_{13/2} \rightarrow {}^{4}I_{15/2}$ transition will be at ~ 1644 nm. This is in agreement with the report on an Er:YSGG inband-pumped laser emitting at 1643 nm [37]. For real ~ 1.5 µm laser applications, concentration of Er^{3+} ions of < 1 at% should be selected to avoid the detrimental influence of strong up-conversion.

For the ${}^{4}I_{11/2} \rightarrow {}^{4}I_{13/2}$ channel, the maximum stimulatedemission cross-section is 0.43×10^{-20} cm² at 2797.1 nm, Fig. 5(c). This emission channel is free of reabsorption losses, so one can expect generation at this wavelength in an Er:YSGG laser.

Table 7	/
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Stimulated-emission cross-sections σ_{SE} for the ${}^{4}I_{11/2} \rightarrow {}^{4}I_{13/2}$ and ${}^{4}I_{13/2} \rightarrow {}^{4}I_{15/2}$ transitions of Er^{3+} ions in various crystals.

Crystal	$\sigma_{\rm SE}$, $10^{-20}~{\rm cm}^2$		Ref.
	${}^{4}I_{11/2} \!\rightarrow {}^{4}I_{13/2}$	${}^4I_{13/2} \!\rightarrow {}^4I_{15/2}$	
Er:YSGG	0.43 2.8	1.20	This paper
Er:YAG	0.56	0.72	[39,40]
Er:GSGG	2.9	-	[32]
Er:YAlO ₃	-	0.55	[40]
Er:YSO	-	1.0	[41]
Er:YLF	1.2	-	[38]
Er:KY ₃ F ₁₀	1.9	-	[32]

Peak stimulated-emission cross-sections σ_{SE} for the ${}^{4}I_{13/2} \rightarrow {}^{4}I_{15/2}$ and ${}^4I_{11/2} \rightarrow {}^4I_{13/2}$ transitions of Er^{3+} ions for Er:YSGG and several Er^{3+} -doped crystals are compared in Table 7. It should be noted that $\sigma_{\rm SE}$ spectrum was never reported for the ${}^{4}I_{11/2} \rightarrow {}^{4}I_{13/2}$ transition of Er^{3+} ions in the YSGG crystal. Previously for the calculation of peak $\sigma_{\rm SE}$ value corresponding to this transition, lifetime of the ${}^{4}I_{11/2}$ upper laser level reported by Dinerman, τ_{exp} =3.4 ms [2], was used. This led to the overestimation of the $\sigma_{ ext{SE}}$ value that was typically considered to be \sim 2.8 \times 10⁻²⁰ cm². However, as in [2] τ_{exp} was determined directly from the PL decay curves for a highly-doped (30 at% Er) crystal, it was much shorter than the radiative lifetime, namely 9.75 ms as determined in the present paper from the J–O modeling. Similar situation for different Er-doped crystals is addressed in details in [32]. For the ${}^{4}I_{13/2} \rightarrow {}^{4}I_{15/2}$ transition, stimulated-emission and gain cross-sections spectra were also not reported for Er:YSGG crystal. However, the obtained peak σ_{SE} values for this transition are in accordance with the ones reported previously for different Er-doped materials, see Table 7.

The measured decay curves for the luminescence from the five lowest excited-states of Er^{3+} ions in YSGG are shown in Fig. 6 (${}^{4}S_{3/2}$ and ${}^{2}H_{11/2}$ levels are treated as a single, thermally coupled level). Relatively high Er concentration should lead to significant concentration guenching and a high rate of non-radiative relaxation in the Er:YSGG crystal. Thus, shortening of the measured lifetime, τ_{exp} , as compared with the radiative one, τ_{rad} , is expected for all excited-states of ${\rm Er}^{3+}$ ions. The measured decay times $au_{
m exp}$ of the luminescence from the ${}^{4}I_{13/2}$ and ${}^{4}I_{11/2}$ states are 2.24 and 1.3 ms, respectively (compare with the corresponding radiative lifetimes, 7.73 and 9.75 ms as determined from the J–O modeling). The value of $\tau_{exp}({}^{4}I_{13/2})$ obtained in the present paper for 38 at% Er:YSGG crystal is shorter than the value reported in [2] for 30 at% Er doped crystal, namely 3.2 ms. For the ${}^{4}I_{9/2}$ - ${}^{2}H_{11/2}$ states, the measured lifetimes are on the order of a few μ s (cf. Table 5). By comparing τ_{rad} for the ${}^{4}F_{9/2}$ state (responsible for red emission) and the thermalized ${}^{4}S_{3/2} + {}^{2}H_{11/2}$ states (responsible for green UCL), the prevalence of red emission in the UCL can be explained. Indeed, $\tau_{rad}(F_{9/2}) = 10.2 \ \mu s$ which is nearly 25 times longer than for the $^4S_{3/2}$ and $^2\dot{H}_{11/2}$ states. In addition, the lifetime of the ${}^{4}I_{11/2}$ state is shorter than that of the ${}^{4}I_{13/2}$ state, so the ESA process $({}^{4}I_{13/2} \rightarrow {}^{4}F_{9/2})$ that populates the ${}^{4}F_{9/2}$ level responsible for red emission will be stronger.

By comparing radiative lifetimes of the excited states $[\tau_{rad} = \Sigma_J A(JJ')]$ and measured decay times for the luminescence from these states, τ_{exp} , we estimated the nonradiative decay-rate constants, $A_{NR} = (1/\tau_{exp}) - \Sigma_J A(JJ')$, see Table 8. The value of A_{NR} is related to the energy gap ΔE between the considered state and the lower-lying state by the equation [42]:

$$A_{\rm NR} = C e^{-\alpha \Delta E} \tag{11}$$

where *C* and α are the constants characteristic of the host material. Eq. (11) is applicable for a constant temperature and concentration of active ions.



Fig. 6. Luminescence decay curves for emissions from the ${}^{4}I_{13/2}$, ${}^{4}I_{11/2}$ (a), ${}^{4}F_{9/2}$ and ${}^{4}S_{3/2}$ (c) excited-states of Er³⁺ ions in the 38 at% Er: YSGG crystal under resonant excitation; (d) energy-gap dependence of the nonradiative decay-rate constants A_{NR} in 38 at% Er:YSGG in a semi-log scale: *points* are the values determined with the measured luminescence lifetimes and the calculated radiative decay rate constants, *line* is the fit through these data with Eq. (11).

Table 8

Energy gaps to the next lower levels, total radiative decay-rate constants, radiative and luminescence lifetimes, and nonradiative decay-rate constants of the lowest five excited states^{*} of Er^{3+} in YSGG.

State	<i>E</i> , cm ⁻¹ [15]	$\Delta E_{\rm min}$, cm ⁻¹	$\sum_{J'}A(JJ'),$ s ⁻¹	$ au_{\rm rad}$, ms	τ_{exp} , ms	$A_{\rm NR}$,*** s ⁻¹
⁴ I _{15/2}	0-502	_	_	_	_	_
$^{4}I_{13/2}$	6553-6872	6370	129.3	7.73	2.24	318.1
$^{4}I_{11/2}$	10,244-	3372	102.6	9.75	1.30	666.6
	10,403					
⁴ I _{9/2}	12,296-	1893	234.2	4.27	0.4	$2.85 imes 10^6$
	12,734					
⁴ F _{9/2}	15,310-	2576	1531	0.65	10.2	9.65×10^4
	15,527					
${}^{4}S_{3/2} + {}^{2}H_{11/2}$	18,407-	2880	4757	0.21	0.4	$2.50 imes 10^6$
. ,	19,367					

* The ${}^{4}S_{3/2}$ and ${}^{2}H_{11/2}$ levels are treated as a single, thermally coupled level. ** $A_{NR} = (1/\tau_{exp}) - \Sigma_{J}A(JJ')$.

In Fig. 6(d), we plotted the obtained values of $A_{\rm NR}$ vs. the minimum energy gap $\Delta E_{\rm min}$ between the excited-states calculated from the known structure of energy levels of ${\rm Er}^{3+}$ ions in the YSGG crystal. In a semi-log scale, this dependence was fitted by a linear law yielding $C=3.4 \times 10^7 {\rm s}^{-1}$ and $\alpha=2.0 \times 10^{-3} {\rm cm}$ constants. The agreement between the calculated $A_{\rm NR}$ values and the best-fitting curve is satisfactory for the ${}^4I_{13/2}$, ${}^4I_{9/2}$, ${}^4F_{9/2}$ and ${}^4S_{3/2}+{}^2H_{11/2}$ states, while for the ${}^4I_{11/2}$ state the calculated $A_{\rm NR}$ value (666.6 s⁻¹) is one order of magnitude lower than one predicted from the linear fit ($\sim 8 \times 10^4 {\rm s}^{-1}$). Thus, simple model described by Eq. (11) that is typically used for the description of nonradiative decay in ${\rm Er}^{3+}$ -doped materials with a relatively low ${\rm Er}^{3+}$ concentrations [43], predicts even stronger shortening of the

luminescence lifetime of the ${}^{4}I_{11/2}$ state for Er:YSGG crystal. However, particularly long τ_{exp} value for this state makes Er:YSGG crystal attractive for laser operation on the ${}^{4}I_{11/2} \rightarrow {}^{4}I_{13/2}$ transition (i.e., as compared with Er:YAG) (Fig. 6).

The deviation of the experimental points on $A_{\rm NR}$ from the linear law is attributed to a very high concentration of ${\rm Er}^{3+}$ ions that could generate more complicated dependence between $A_{\rm NR}$ and ΔE . Indeed, the considered $N_{\rm Er}$ value (4.82 × 10²¹ at/cm³) should be compared with the so-called quenching concentration $N_{\rm q}$ that corresponds to a reduction of the luminescence lifetime $\tau_{\rm exp}$ with respect to the radiative one $\tau_{\rm rad}$ by a factor of 2, $\tau_{\rm exp} = \tau_{\rm rad}/$ $[1 + (N_{\rm Er}/N_{\rm q})^2]$ [44]. For ${\rm Er}^{3+}$ ions in YAG, $N_{\rm q} \sim 3 \times 10^{21}$ at/cm³ [45] (for the ${\rm Er}^{3+}$:YSGG crystal, these data are not presented in the literature).

More significant shortening of $\tau_{\rm exp}$ with respect to $\tau_{\rm rad}$ for the ${}^{4}I_{11/2}$ state as compared with the ${}^{4}I_{13/2}$ state can be understood with Eq. (11) and the values of energy gaps ΔE_{min} for these states that are 3372 and 6370 cm⁻¹, respectively. If considering multiphonon mechanism of the non-radiative decay, this means that \sim 5 and 9 phonons are required to depopulate theses states (here we consider the maximum vibrational frequency of YSGG, $\nu_{\rm max}$ =752 cm⁻¹ [46]). Thus, for the ${}^{4}I_{11/2}$ state this process should have much higher probability. Another mechanism of shortening of the τ_{exp} value can be energy-transfer to the impurities ions that in enhanced with the increase of the Er^{3+} concentration [45]. The probability of this energy-transfer can be different for the ${}^{4}I_{11/2}$ and ⁴I_{13/2} states depending on if they are resonant in energy to the impurity states; in addition, this process is strongly dependent on the growth method and particular composition of the considered sample [45].

4. Conclusions

We report on a comprehensive spectroscopic study of a highlydoped 38 at% Er:YSGG crystal. Optical absorption and luminescence of Er³⁺ ions is studied. The maximum absorption crosssection for the ${}^{4}I_{15/2} \rightarrow {}^{4}I_{11/2}$ transition is $\sigma_{abs} = 0.46 \times 10^{-20}$ at 965.8 nm. Radiative lifetimes of all excited states of the Er³⁺ ion from ${}^{4}I_{13/2}$ to ${}^{2}H_{9/2}$, branching ratios and probabilities of radiative transitions from these states are determined using the Judd-Ofelt theory. Radiative lifetimes of the ${}^{4}I_{13/2}$ and ${}^{4}I_{11/2}$ excited states for Er^{3+} ions in YSGG crystal are 7.73 ms and 9.75 ms, respectively. Using these relevant spectroscopic data, stimulated-emission cross-section spectra are evaluated for $\sim 1.5 \,\mu m \, (^4 I_{13/2} \rightarrow ^4 I_{15/2})$ and 3 μ m (⁴I_{11/2} \rightarrow ⁴I_{13/2}) transitions. For the ⁴I_{11/2} \rightarrow ⁴I_{13/2} channel, maximum stimulated-emission cross-section the $0.43 \times 10^{-20} \text{ cm}^2$ at 2797.1 nm. The role of non-radiative relaxation on the shortening of luminescence lifetimes of lower excitedstates of Er³⁺ is discussed.

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