604-nm high-order vortex beams directly generated from a Pr:YLF laser with a cavity-loss-induced gain switching mechanism

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HIGHLIGHTS

- First demonstration of 604-nm vortices directly generated from a Pr:YLF laser.
- Topological charge up to three was achieved through designated cavity design.
- Cavity-loss-induced gain switching mechanism between 604 and 607 nm emission.
- Output power reached 470, 230, and 60 mW for the 1st-, 2nd-, and 3rd-order vortex.
- Slope efficiencies were 24.5\%, 17.5\%, and 11.4\%, respectively.

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ABSTRACT

In this work, we demonstrated, for the first time to the best of our knowledge, high-order vortex beams at 604 nm that were directly emitted from a Pr:YLF crystal laser. By combining a blue-diode-pumped \(\text{v}\)-type cavity for controllable Gouy phase introduction and off-axis crystal rotation for high-order HG modes generation, topological charged 604-nm vortex lasers were attained up to the third order. Furthermore, the vortex beams were found to be lasing at 604 nm that was often deemed less prone to lase compared with 607-nm in the same energy manifold. By a detailed spectroscopic study and rate equation analysis, we proposed and confirmed that the 604-nm transition of Pr:YLF crystal could be favorable in the vortex beam generation by a cavity-loss-induced gain switching process, in which the net gain at 604-nm could surpass that of 607-nm as the cavity loss was amassed beyond a threshold value.

1. Introduction

High-order optical vortices, carrying more than one topological charge for each photon, are ideal light sources for macroscopic quantum entanglement measurement \cite{1}, angular remote sensing \cite{2}, precise spatial measurement \cite{3}, and laser printing of chiral plasmonic nanojets \cite{4}. Optical vortices directly generated from lasers, which constitute cavity eigenstates and possess inherently superior beam quality, are preferable choices \cite{5}. Higher-order vortex beams in the orange that is at the absorption band of certain metal phthalocyanines, uranium-doped CaF\(_2\) crystals, and hybrid liposome/Au nanoparticles, may offer new perspectives for applications in nonlinear absorption spectroscopy \cite{6}, crystallographic characterization \cite{7}, and biomedical photonics \cite{8}.

One of the promising and well-studied gain media for orange lasers is the praseodymium-doped yttrium lithium fluoride (Pr:YLF) \cite{9–14}. To realize optical vortex beams, off-axis pumping scheme has been widely used in generating high-order Hermite-Gauss (HG) modes that can be transformed to corresponding high-order Laguerre-Gauss (LG) modes by external mode converters \cite{15–17}. Such approach was recently exploited to produce red and orange vortex beams directly from a Pr:YLF laser cavity, however, the vortices achieved were limited to first-order vortex beams \cite{18,19}.

In this paper, we demonstrated direct emission of high-order LG vortex beams in the orange spectra from a Pr:YLF laser utilizing an equivalent off-axis pumping scheme combined with a robust \(\pi/2\) Gouy phase introduction. Furthermore, upon studying the emitted spectra of LG vortex beams up to the 3rd order, we discovered that the wavelength was centered at 604 nm, instead of the commonplace 607 nm in the orange. Based on a thorough spectroscopic study and rate-equation analysis, we confirmed that, to the contrary of common notions, the net gain of 604-nm transition at room temperature could be higher than...
that of 607-nm by a simple cavity loss management when the total loss was beyond a threshold value, resulting in a swift gain switching from 607 to 604 nm with the proper setup.

2. Experimental setup

To directly generate orange LG vortex beams, as illustrated in Fig. 1, we utilized a three-mirror v-type Pr:YLF cavity. The gain medium was a cubic a-cut crystal with a relatively low doping concentration of 0.3 at.%. The low doping level was to not only reduce the thermal load and avoid the risk of crystal fracturing [14], but also weaken the ground-state re-absorption [10]. A relatively large crystal thickness of 10 mm was consequently utilized to increase the pump absorption. The Pr:YLF crystal was polished at both ends, wrapped in indium foils on the side, and mounted on a copper heatsink that was Peltier cooled to 12 °C. The crystal was integrated onto a kinematic mount with two motorized actuators, which provided an angular precision of 6 arc second to stimulate the high-order transverse modes. The pump diodes and beam shaping system were similar as in [20], except that the diode temperature was set at 21 °C to optimize pump absorption. The v-type cavity was carefully constructed to effectively introduce an appropriate Gouy phase difference to high-order beams, which was critical for the HG to LG mode conversion [21]. The planar input mirror (IM) was coated with high transmission (> 98%) from 436 to 455 nm for the pump, and transmission of 72% at 522 nm to suppress possible lasing. The IM was also highly reflective (> 99.8%) from 592 to 620 nm. The folding mirror (FM) was coated of high reflection (> 99.8%) from 560 to 611 nm and high transmission (> 60%) from 631 to 738 nm to suppress possible lasing at 640 and 721 nm. The third mirror, partially reflective with ~13.6% transmission from 600 to 610 nm, was chosen as the output mirror (OM). To characterize the output beam, an improved Fizeau interferometer [22] in the orange spectral region was utilized to generate spherical wave interference, which was followed with a neutral density filter and a high-resolution CCD camera for interferogram recording.

3. Results and discussion

For vortex beam generation, LG modes can be converted from HG modes by superimposing a \( \pi/2 \) Gouy phase, while HG modes can be acquired by lowering the threshold below that of Gaussian mode with proper crystal rotation [23]. The set of cavity parameters, \( l_1, l_2, \) and \( \theta \), required to bring the \( \pi/2 \) Gouy phase into the laser, can be calculated by the ABCD matrix law [21] with results plotted in Fig. 2(a). In general, \( l_1 \) increases with the decrease of \( \theta \), and \( l_2 \) increases with both \( l_1 \) and \( \theta \) decreasing. On the other hand, the value of \( \theta \) is closely related to the cavity modal size. To achieve higher laser efficiency, the signal beam inside the gain crystal should be optimized for maximal overlapping with the pump beam. Thus in our design, \( \theta \) was chosen to be 46°. The variation of \( l_2 \) and tangential/sagittal waist radius (\( \omega_{0T}/\omega_{0S} \)) in the crystal versus \( l_1 \) were plotted in Fig. 2(b). It was revealed that a maxima of \( l_2 \approx 58 \) mm existed at \( l_1 \approx 33 \) mm, resulting in \( \omega_{0T} = \omega_{0S} \approx 38 \) \( \mu \)m that matched well with the pump mode inside. Therefore, \( l_1 \) and \( l_2 \) were set at around 33 and 58 mm, respectively, to initiate the vortex beam lasers.

A. First-order vortex beam generation

To initiate the laser operation, TEM\(_{00}\) mode (Fig. 3(a)) was first obtained by aligning the end surfaces of Pr:YLF crystal perpendicular to the pump beam and adjusting IM and OM near the FM center. Next, by consecutively rotating the crystal both in the tangential and sagittal plane by an angle of \( \approx 2.2° \), i.e., indicated by the orange arrow in the bottom left inset in Fig. 1, the diagonal HG\(_{01}\) mode (Fig. 3(c)) was achieved. In the next step, \( l_1 \) and \( l_2 \) were set at the calculated values and

![Fig. 1. Schematic setup of the blue-diode-pumped 604-nm vortex laser with topological charge up to 3.](image1)

![Fig. 2. Cavity parameters design for \( \pi/2 \) Gouy phase shift. (a) Relationship among cavity parameters \( l_1, l_2, \) and \( \theta \); (b) Variation of \( l_2 \) and signal beam waist versus \( l_1 \).](image2)

![Fig. 3. The intensity profiles and corresponding interferograms for (a, b): TEM\(_{00}\); (c, d): diagonal HG\(_{01}\); (e, f): LG\(_{0,+,1}\); and (g, h): LG\(_{0, -,1}\) modes.](image3)
The beam spots of LG vortex beams were also inverted in a similar manner as the 1st-order modes. Illustrated very clear spiral fringes with both topological charge \( l = -1 \) and confirmed the validity of controllable chirality with our vortex lasers. The interferograms of TEM\(_{10}\) and diagonal HG\(_{01}\) modes were also inspected and displayed in Fig. 3(b) and (d), respectively, both of which exhibited ring-shaped interference patterns with no spiral structure and indicated zero carried OAM.

B. High-order vortex beam generation

Moving forward with the 1st-order vortices, we further rotated the YLF crystal and adjusted the cavity parameters to achieve high-order vortex beams. The 2nd-order vortex beam, as shown in Fig. 4(a), was observed when the total tilt angle was tuned to 5.4°, while \( l_1 \) and \( l_2 \) were adjusted to ~34 and 56 mm, respectively. The 3rd-order vortex beam, as shown in Fig. 4(e), was observed when the total tilt angle was tuned to 6.8°, while \( l_1, l_2 \), and \( \theta \) were adjusted to ~33 mm, 59 mm, and 45°, respectively. The corresponding interference patterns illustrated very clear spiral fringes with both topological charge \( l = +1 \) and \( l = +3 \) in Fig. 4(b) and (f). Furthermore, the handedness of vortices were also inverted in a similar manner as the 1st-order modes. The beam spots of LG\(_{0-2}\) and LG\(_{0-3}\) modes were shown in Fig. 4(c) and (g), respectively. Their interference patterns were displayed in Fig. 4(d) and (h), respectively. We noted a small ellipticity existed in the beam spots and we believe it was due to the astigmatism caused by the cavity folding and crystal rotation. We also noted that in achieving a larger topological charge, \( l_1 \) and \( \theta \) were decreased slightly while \( l_2 \) was increased larger than \( l_1 \). Such experimental observations were consistent with our theoretical predictions in Fig. 2(a).

C. The laser emission spectrum and power

In recording the emission spectra of vortex lasers, an intriguing observation was revealed during mode conversion. First, the central emission wavelength was located at 607.0 nm for the TEM\(_{00}\) mode, as expected; however, it was shifted to 604.2 nm for the HG\(_{01}\) and LG\(_{01}\) (both chiralities) modes as well as higher topological charges up to the 3rd order, as shown in Fig. 5(a). As we mentioned earlier, such an abrupt switch in the emitted spectra was against the common observations for regular orange lasers with Pr:YLF crystals. The physical explanation to this interesting phenomenon will investigated in detail in the next section.

Regarding the emitted vortex laser power, the maximum continuous-wave (cw) output power for the 1st-, 2nd-, and 3rd-order 604-nm laser reached 470, 230, and 60 mW, respectively, under an absorbed pump of 2.8 W. The pump thresholds were 0.76, 1.46, and 2.29 W, respectively, and accordingly the slope efficiencies were 24.5%, 17.5%, and 11.4%, respectively. All three outputs exhibited no obvious thermal rollover and were only limited by the available pump power, as shown in Fig. 5(b). The degradation of laser efficiencies for higher-order vortex modes could be attributed to two main reasons. The first was that higher-order vortex beams had larger hollow areas and smaller mode sizes inside the gain crystal, which reduced the signal-pump overlapping efficiency. The second was due to the higher diffraction losses at the crystal surfaces for higher-order modes with larger tilt angles.

4. Validation of the cavity-loss-induced gain switching and emission spectrum change

The switching of the emitted laser spectrum from 607 to 604 nm along with the vortex beam occurrence has led us to investigate on the spectroscopic characteristics in Pr:YLF lasing. It is well known that Pr:YLF crystal has two close emission peaks in the same energy manifold at 604 and 607 nm, respectively [11]. Traditionally, the perception is that the 607-nm transition is prone to lasing because it has higher gain and lower loss comparing with those of 604-nm [12]. This pre-conceived notion has been supported by several experimental observations [13,14] including the recently demonstrated Pr:YLF vortex laser at 607 nm [18]. On the other hand, for Pr:YLF to laser at 604 nm, extra resources have to be employed including cryogenic facilities [9], Fabry–Perot etalons [10], and saturable absorbers [24] etc., resulting in complex, costly, and less efficient laser systems. There has been little reported studies for a room-temperature Pr:YLF laser preferentially emitting at 604 nm without some delicate external measures.

We first looked into the polarization-resolved spectroscopy for the \(^3\)H\(_4\)→\(^2\)D\(_2\) ground-state absorption and \(^3\)P\(_0\)→\(^3\)H\(_4\) emission processes to characterize the transition strength at 604 and 607 nm. The absorption spectra were completed with a visible spectrophotometer (PerkinElmer Inc., Lambda 850). Although this absorption was considered spin forbidden and non-resonant with low cross-sections [12,13], our inspection revealed the absorption cross-sections at 604 and 607 nm were \(6.7 \times 10^{-22}\) cm\(^2\) and \(1.2 \times 10^{-22}\) cm\(^2\), respectively, which were consistent with previous reports [12]. Next, the emission spectra were carefully recorded by pumping a cubic Pr:YLF crystal at one edge and collecting the emission from a perpendicular side to minimize possible re-absorption. The emission data were recorded with an optical spectrum analyzer (Yokogawa, AQ6373B) in the visible and the emission cross-sections were derived to be 19.6 × 10\(^{-20}\) cm\(^2\) and 15.7 × 10\(^{-20}\) cm\(^2\) at 604 and 607 nm, respectively. To note, our emission cross-section at 604 nm was double as previously reported data [13], while similar at 607 nm. Our spectroscopic data indicated that while the 604-nm transition possibly possessed a slightly higher gain, the 607-nm gain was substantially less (~5 times less) influenced by the ground-state absorption. This inherent absorption could be substantial and effectively prevent the 604-nm lasing with 607-nm gain present. This
perspective was obviously met with earlier results [13] where cw 607-nm lasing first occurred at a low pump level, and cw 604-nm lasing appeared only after the pump exceeded a high level such that both transitions could overcome the inherent losses from the ground-state absorption.

To understand the gain competition process between the two orange wavelengths, a generic rate equation analysis was conducted, as listed in Eq. (1), with an assigned general cavity loss $\gamma$ [25]. The photon density is $\phi$, the excited-state population density is $N_E$, the ground-state population density is $N_g$, and $N = N_E + N_g$ is the total Pr$^{3+}$ population density. The subscripts 1 and 2 denote the 604- and 607-nm transition, respectively.

$$\begin{align*}
\frac{d\phi_1}{dt} &= \frac{\sigma_p}{\pi} [2L(\sigma_{a1}N_E - \sigma_{a2}N_g) - \gamma], \\
\frac{d\phi_2}{dt} &= \frac{\sigma_p}{\pi} [2L(\sigma_{a2}N_E - \sigma_{a1}N_g) - \gamma], \\
\frac{dN}{dt} &= \frac{\sigma_p e P}{h c \gamma} N_g - (\phi_1 \sigma_{a1} + \phi_2 \sigma_{a2})cN_E - \frac{N}{\tau},
\end{align*}$$

(1)

In the rate equations, $t_c$ is the cavity round-trip time, $L$ is the crystal length, $c$ is the speed of light in vacuum, and $\tau_f$ is fluorescence lifetime. Here $\sigma_{a}$ and $\sigma_{e}$ denote the emission and absorption cross-section, respectively. For the pump laser, $\lambda_p$, $P_p$, $\sigma_{a0}$, and $\sigma_{p0}$ are the wavelength, absorbed power, absorption cross-section, and beam radius inside the crystal, respectively. Base on the rate-equation set, we simulated the gain competition process between the two transition lines with parameters listed in Table 1.

The simulation results, i.e., the photon density versus loss term $\gamma$, were plotted in Fig. 6. It was clearly observed there existed a steep turning point that triggered the gain switching between 604- and 607-nm transitions. The critical loss $\gamma$ was found at 17.3%, depending on the parameters chosen. Note that it was the only switching point for $\gamma$ from zero to 100%, as shown in the inset of Fig. 6, and the 604-nm gain prevailed afterwards. This general loss $\gamma$ was mainly composed of the reflection and absorption losses from the crystal, and output coupler loss. The obtained critical loss provided a good guideline for the subsequent vortex laser design aiming at 604-nm high-order modes with expected higher cavity loss.

To validate the theoretical predication with our experimental observations, we hereby looked into the detailed losses in our cavity set. For the TEM$_{00}$ mode with collinear alignment, the reflected beam at the crystal facet was always injected back into the cavity that led to a maximal internal loss below 1% for a well-aligned cavity [27]. The utilized OM transmittance was 13.6%, thus for the TEM$_{00}$ mode the cavity loss was about 15.6%, which was below the critical loss of 17.3% and in favor of 607-nm transition. On the other hand, high-order transverse modes, including the 1st- and higher-order vortices, generally experienced more severe losses by the tilted crystal and cavity mirrors. In a cavity round-trip, the laser beam would pass through the crystal facets for a total of four times. Since the crystal was tilted, part of the reflected beam would eventually exit the resonator after a few bounces. The total reflection loss, considering the Fresnel reflection was $\sim 3.7\%$ at one Pr:YLF crystal facet (uncoated with a refractive index of 1.476 at 604 nm and 1.453 at 607 nm) and the small tilt angle, was estimated to be no less than 4% under proper assumption. Thus, the total cavity loss was amassed to be 18.6% or higher, which was beyond the threshold in favor of the 604-nm transition. Therefore, our experimental observations were in good agreement with the theoretical predictions. Without this loss management, vortex beams would still emit at the preferable 607 nm in a simple linear cavity [18].

5. Conclusion

To conclude, in this paper we presented a diode-pumped Pr:YLF laser that directly generated high-order vortex laser beams at 604 nm. Utilizing an elaborate design to superpose an intra-cavity π/2 Gouy phase shift and a delicate cavity loss management that preferred the 604-nm transition line, LG vortex laser emissions of both chiralities were achieved from HG modes conversion. Vortex beams up to the 3rd-order were attained directly out of the laser cavity with appreciable maximal output powers of 470, 230, and 60 mW for the 1st-, 2nd-, and 3rd-order, respectively. We validated the emission wavelength at 604 nm of the vortex beams by a thorough spectroscopic study and rate-equation analysis in the orange laser transition, and revealed that by a controlled loss mechanism the 604 nm transition could have a stronger net gain than that of the 607-nm for the direct vortex lasers. Further exploration to achieve even higher-charged vortices extending to visible wavelengths such as green and deep red, as well as to pulsed laser operations are currently ongoing.

CRediT authorship contribution statement

Saiyu Luo: Conceptualization, Methodology, Software, Formal analysis, Investigation, Writing - original draft, Visualization. Zhiping Cai: Validation. Chuanxiang Sheng: Resources, Funding acquisition. Li Li: Writing - review & editing, Supervision, Funding acquisition, Project administration. Qian Chen: Resources, Funding acquisition.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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